



University of British Columbia  
Department of Mathematics

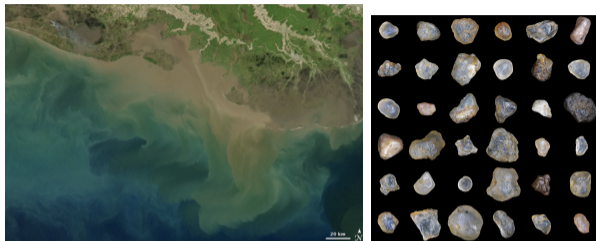
# Dynamics and Wakes of a Fixed and Freely Moving Angular Particle in an Inertial Flow

Basilisk (Gerris) User's Meeting 2023

G. GAI, A. Wachs

- 1 Introduction
- 2 Flow past An Angular Particle
- 3 Freely Settling of A Tetrahedron
- 4 Conclusions and Perspectives

# Angular Particles in Fluids

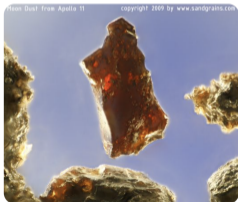


## Particle-laden flows

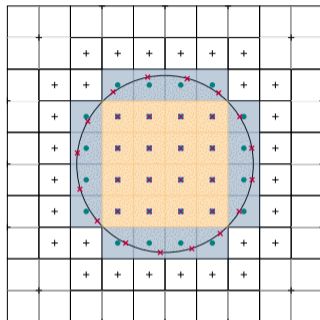
- Sedimentation in rivers
- Particulate air pollution
- Coal & biomass gasification, etc.

## Angular particles

- Complex shapes, sharp edges
- Broad range of size and density
- Rotation, unsteady dynamics



# DLM/FD and Adaptive Mesh Refinement



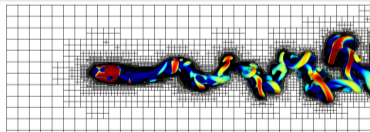
- × Lagrangian multiplier
- Interior points
- Boundary points
- + Fluid nodes

## Combined weak formulation

- $\int_{\Omega} \left( \frac{\partial \vec{u}}{\partial t} + (\vec{u} \cdot \nabla) \cdot \nabla \vec{v} \right) \cdot \vec{v} d\mathbf{x} - \int_{\Omega} p \nabla \cdot \vec{v} d\mathbf{x} + \int_{\Omega} \mu_f \nabla \vec{u} : \nabla \vec{v} d\mathbf{x} = - \int_P \boldsymbol{\lambda} \cdot \vec{v} d\mathbf{x}$
- $\int_{\Omega} -q \nabla \cdot \vec{u} d\mathbf{x}$
- $\left( 1 - \frac{\rho_f}{\rho_p} \right) M \left( \frac{d\vec{U}}{dt} - \vec{g} \right) \cdot \vec{V} - \vec{F}'_i \cdot \vec{V} = \int_P \boldsymbol{\lambda} \cdot \vec{V} d\mathbf{x}$
- $\left( 1 - \frac{\rho_f}{\rho_p} \right) \frac{d\vec{I}\boldsymbol{\omega}}{dt} \cdot \boldsymbol{\xi} - \vec{T}' \cdot \boldsymbol{\xi} = \int_P \boldsymbol{\lambda} \cdot (\boldsymbol{\xi} \times \vec{r}) d\mathbf{x}$
- $\int_P \vec{v} \cdot (\vec{u} - (\vec{U} + \boldsymbol{\omega} \times \vec{r})) d\mathbf{x}$

## Octree mesh refinement

- Criterion: velocity gradient
- Smallest grid size on surface



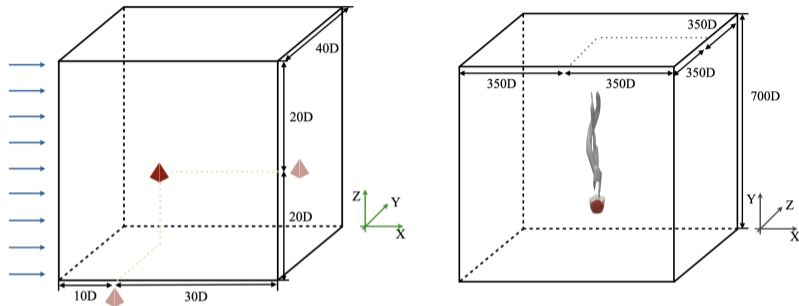
G. Gai & A. Wachs, Powder Technol., 2023



# Flow past An Angular Particle



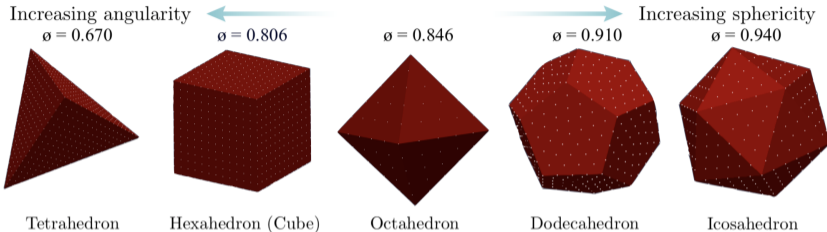
# Fixed (left) and Settling (right) Particle



## Numerical set-up

- Cubic computational domain of size  $40D$  (fixed) and  $700D$  (settling)
- Octree refinement level:  $n_l = 12 \sim 15$ ,  $32 \sim 100$  pts/ $D$

# Platonic Solids



## Three angular positions

### Lagrange multiplier distribution

- Platonic solid with increasing sphericity
- Homogeneous distribution

Edge (E)



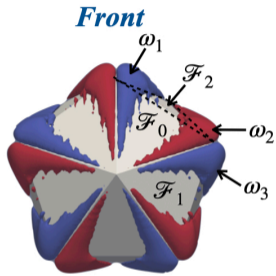
Face (F)



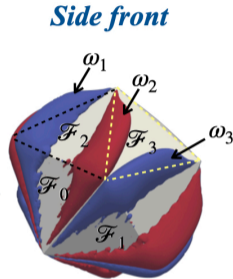
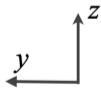
Vertex (V)



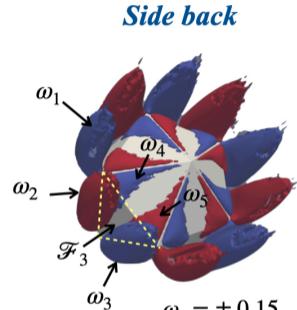
# Vortex Generation on An Angular Particle



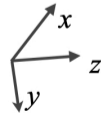
$$\omega_x = \pm 0.8$$



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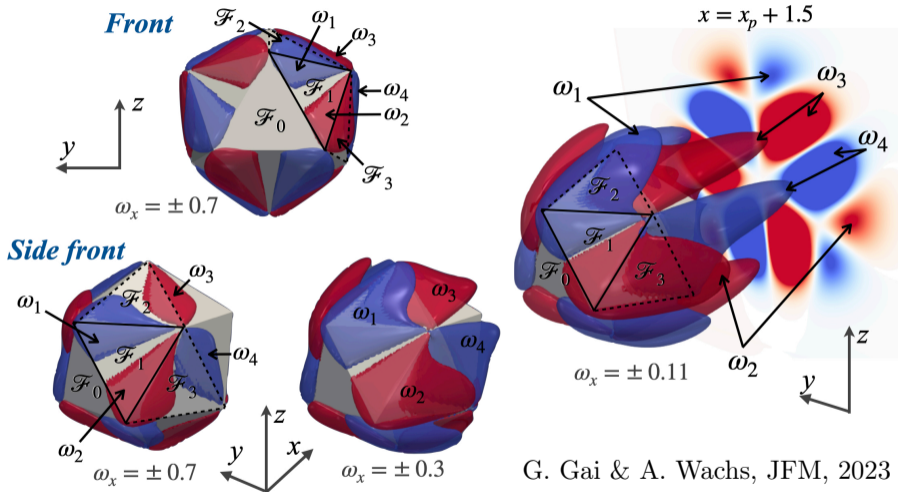


$$\omega_x = \pm 0.15$$



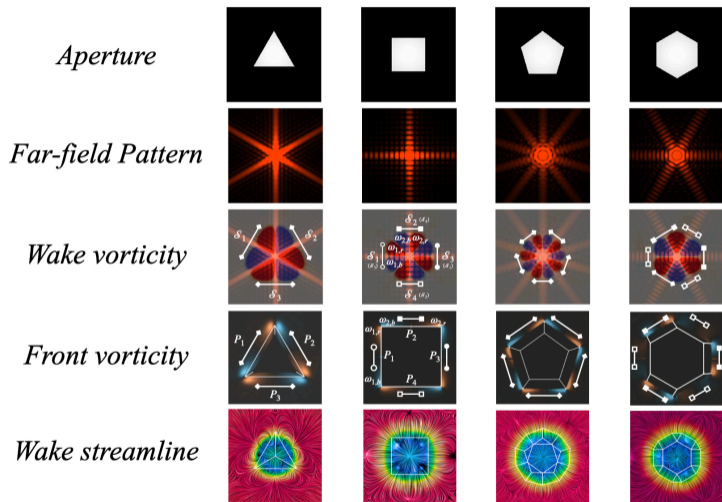


# Vortex Generation on An Angular Particle



G. Gai & A. Wachs, JFM, 2023

# Analogy to Optic Diffraction



## Analogy to Optic Diffraction

- Same symmetry axes
- Imaging of opaque particle
- Deterministic pattern  
dependent on front surface

# Symmetry Breaks: Interaction of Face Induced Vortices

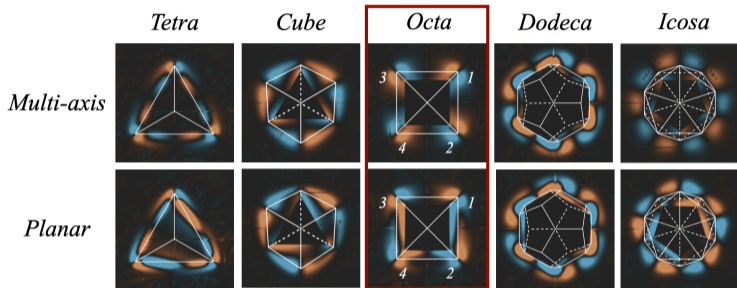
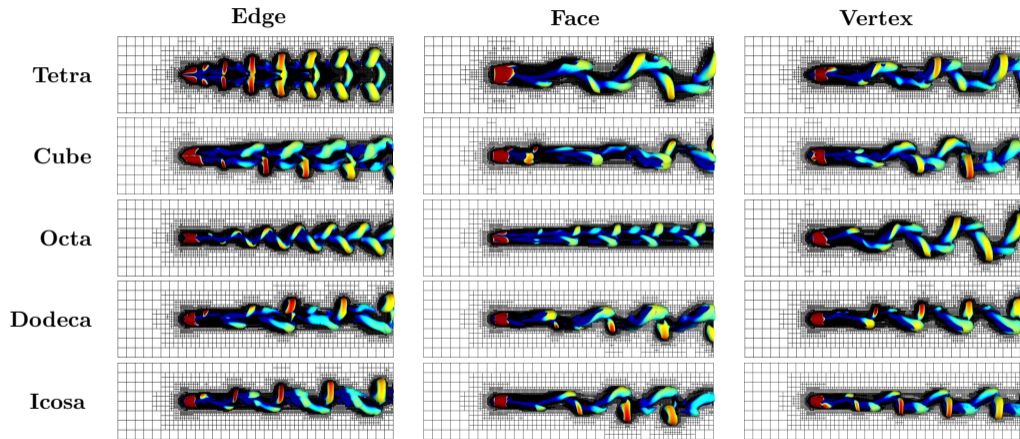


Figure: Stream-wise component of vorticity  $-0.5 < \omega_x < 0.5$  on the rear surface of the Platonic particles: from multi-axis symmetry to planar symmetry;  $\omega_x > 0$  in orange and  $\omega_x < 0$  in blue.

## Symmetry breakup mechanism

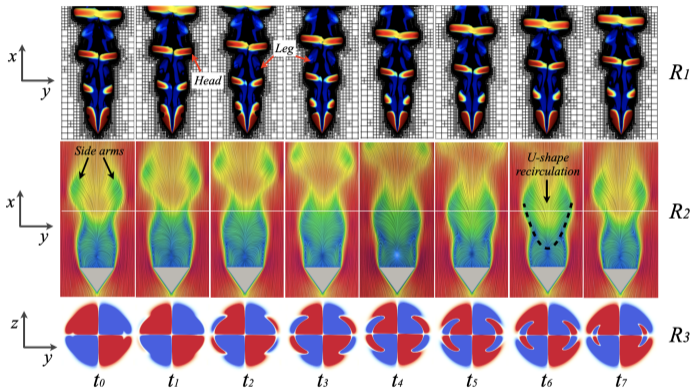
- Opposite-signed vortex pairs from front surface leading edges
- Repulsion of opposite sign, fusion of the same sign
- Vortex arm on the particle rear surface

# Vortex Shedding Patterns



G. Gai & A. Wachs, Part1 & Part2, PRF, 2023

# Double-Hairpin Vortex Shedding



## Double symmetric shedding

- Edge tetrahedron
- Twice shedding frequency
- Planar symmetric

## Shedding dynamics

- Front surface splitting stream
- Rear surface converging
- Unique shape of recirculation

# Drag and Lift Coefficients

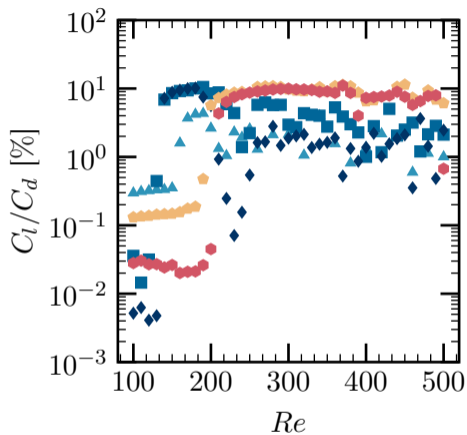
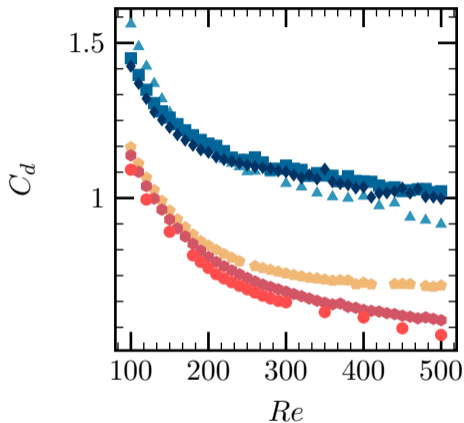


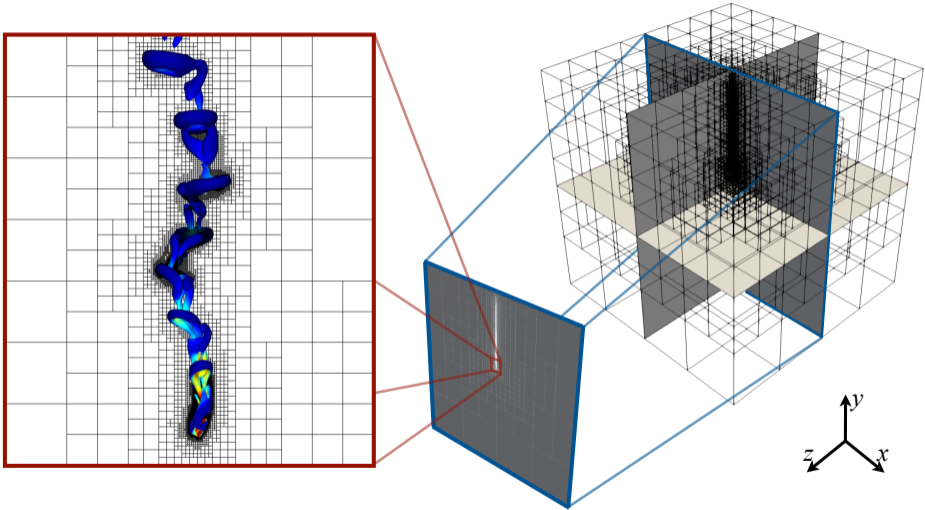
Figure: Drag coefficient  $C_d$  evolution in  $Re$ : TV ( $\blacktriangle$ ), CV ( $\blacksquare$ ), OV ( $\blacklozenge$ ), DV ( $\blacklozenge$ ), IV ( $\bullet$ ) and S ( $\bullet$ ).

Figure: Lift-drag ratio  $C_l/C_d$  as a function  $Re$ : TV ( $\blacktriangle$ ), CV ( $\blacksquare$ ), OV ( $\blacklozenge$ ), DV ( $\blacklozenge$ ), IV ( $\bullet$ ).

# Freely Settling of A Tetrahedron



# A Settling Platonic Particle in an Unbounded Fluid





# A Settling Tetrahedron



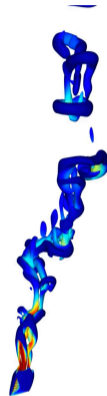
$Ga = 50$



$Ga = 90$



$Ga = 140$



$Ga = 300$

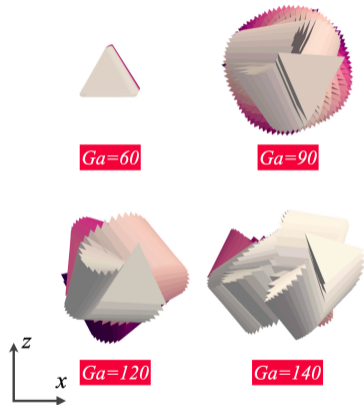
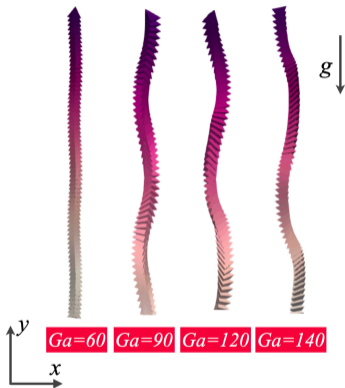
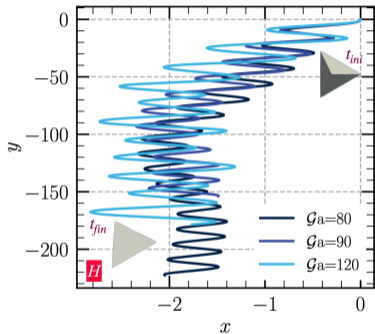
## Steady settling

- Stable: face downwards
- Maximize drag
- Minimize settling velocity

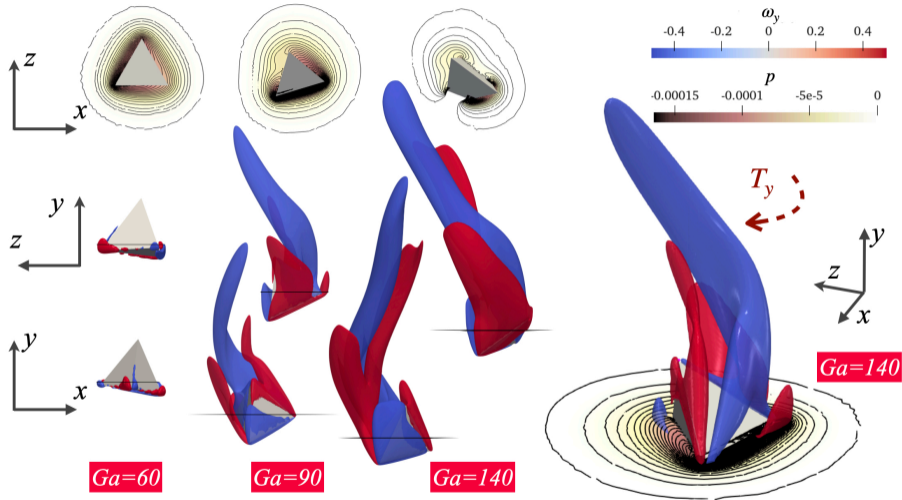
## Double helix vortex

- Rotation enhanced
- Strands elongated with  $Ga$

# Stable Angular Position in the Helical Settling



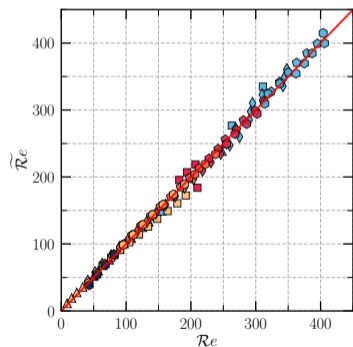
# Helical Settling and Vortex Structure



# Empirical Correlations Based on DNS

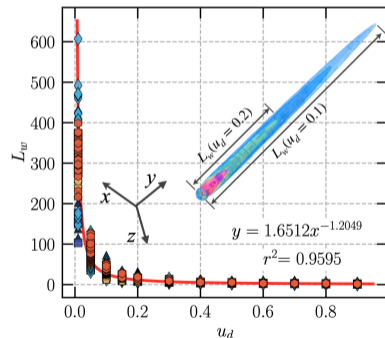
## Settling $Re$

- $\widetilde{Re} = 2.573\phi Ga - 0.916Ga - 0.032 \exp(7.503\phi)$



## Wake length $L_w$

- $L_w = 1.6521u_d^{-1.2049}$ ,  $u_d = u_{crit}/u_{set}$



G. Gai & A. Wachs (In preparation), 2023



# Conclusions & Perspectives

## Conclusions:

- Vorticity structure serves as image of the front surface
- Wake symmetry breakup due to vortex merging
- Rich vortex shedding patterns
- Rich path instability and settling regimes

## Perspectives:

- Magnus effect of a rotating Platonic particle
- Free/turbulent suspensions of Platonic solids



Thank you!

