



# Gerris: a Powerful Modeling Tool for Capillary Flows

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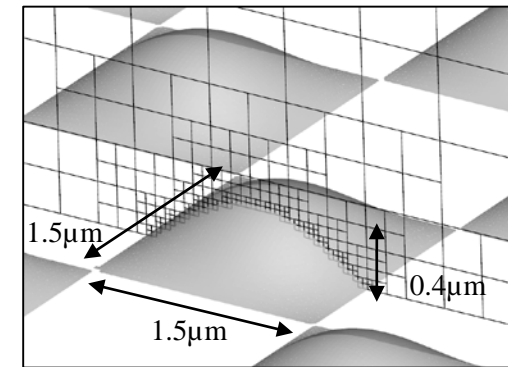
Vancouver, WA



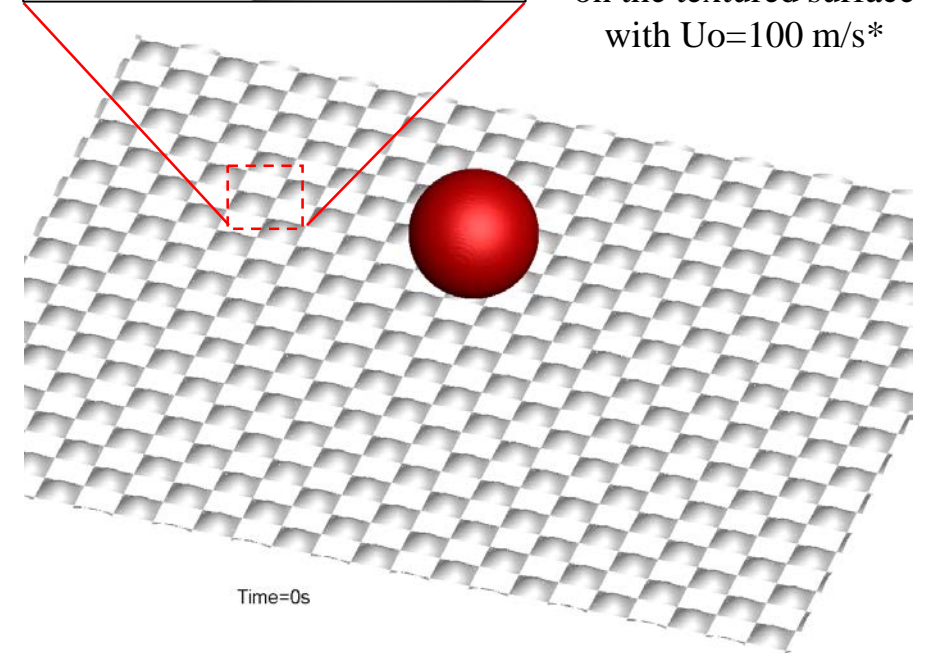
# Outline

- How do I get started with Gerris
- Droplet formation in Inkjet process
- Capillary flow in low-gravity
- Droplet-media interaction
- Future work

Details of the rough surface



A simulation example of  $5\mu\text{m}$  droplet impact on the textured surface with  $U_0=100\text{ m/s}^*$

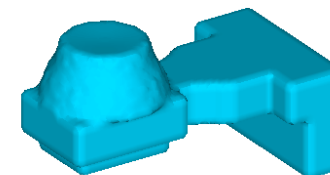
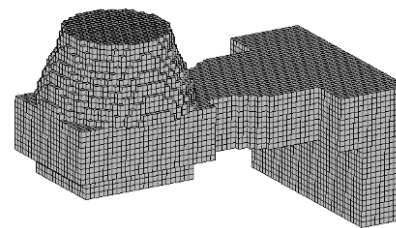


# How do I get started with Gerris

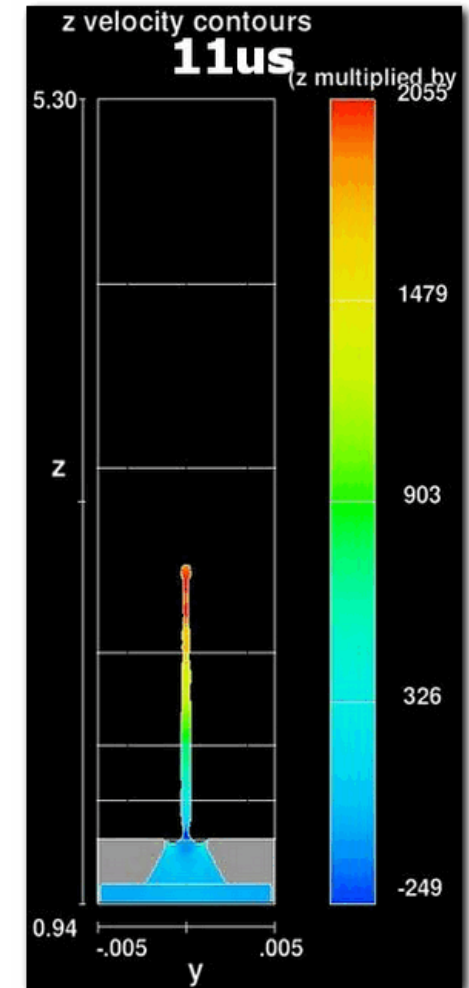
HP's drop-ejection simulation tool: CFD3\*

- Uniform Cartesian grid
- Stair-step method for solid geometry
- Navier-Stokes for liquid phase
- Drive-bubble dynamics
- Contact angle model
- Algebraic calculation based Volume of Fluid
- Height-function for curvature calculation
- Surface-tension directly applied to interface cells

*Original CFD3 has a problem in conserving the momentum!*



CFD3 simulation



Flow3D simulation

\*H. Tan, et al., Numerical simulation of droplet ejection of thermal inkjet printheads. *International Journal for Numerical Methods in Fluids*, 77(9), 544-577, 2015.

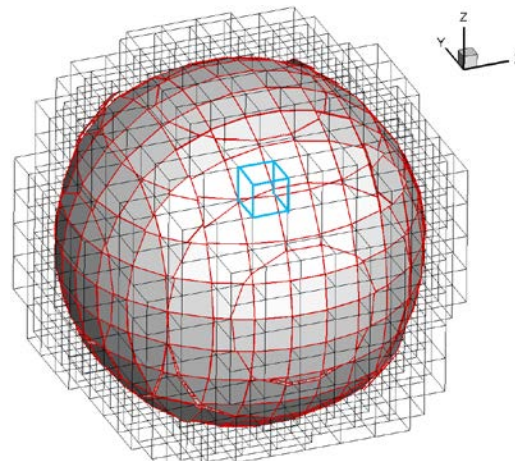
H. Tan, et al, Validation of an in-house 3D free-surface flow solver in inkjet printing, *the 2<sup>nd</sup> ASME Verification and Validation Symposium*, May 22-24, Las Vegas, Nevada, 2013.



# How do I get started with Gerris

- Curvature calculation for under-resolved cells  
paraboloid-fitted method<sup>[1]</sup>
- Geometrical calculation based VOF  
Piecewise Linear Interface Calculation<sup>[2]</sup>

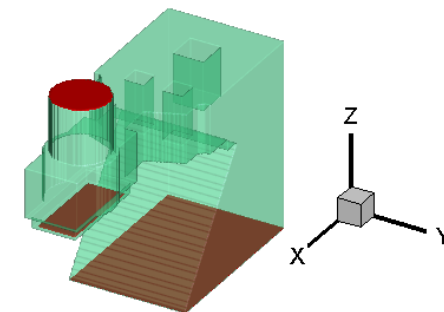
		.1	.2	.1	.01		
.1	.94	1	1	1	.97	.3	
.94	1	1	1	1	1	.98	.2
1	1	1	1	1	1	1	.8
1	1	1	1	1	1	1	.92
.95	1	1	1	1	1	1	.8
.4	.97	1	1	1	1	.95	.1
	.2	.6	.8	.6	.4	.01	



$\kappa$  (height function): -0.373  
 $\kappa$  (parabola-fitting): 0.404  
 Analytical: 0.42

[1]Popinet, S., An accurate adaptive solver for surface-tension-driven interfacial flows. *Journal of Computational Physics*, 2009. **228**(16): p. 5838-5866.

[2]Gueyffier, et al., Volume-of-Fluid Interface Tracking with Smoothed Surface Stress Methods for Three-Dimensional Flows. *Journal of Computational Physics*. **152**(2), 423-456, 1999.



Time = 2.50e-009s



# How do I get started with Gerris

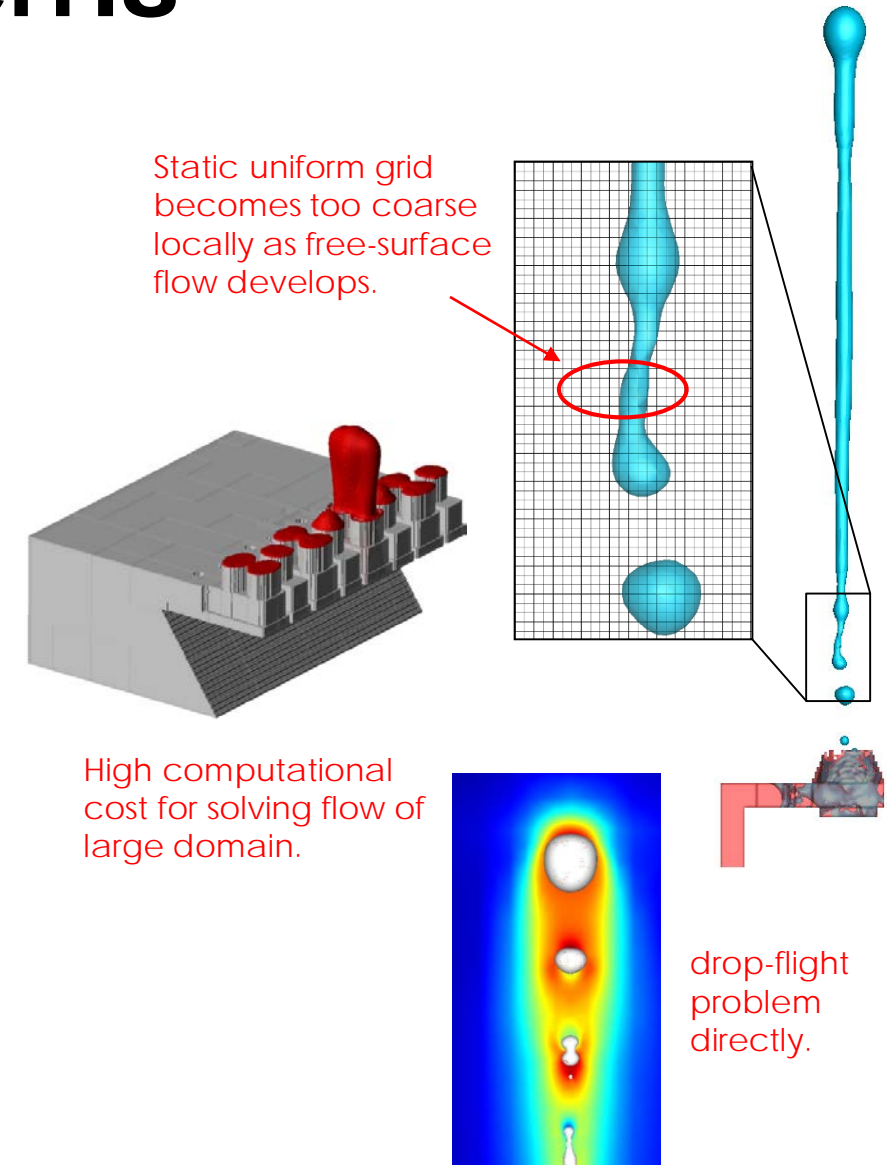
Can Gerris be used to simulate droplet ejection in thermal inkjet process?

Need to know...

- Various numerical methods implemented in Gerris, including NS solver, VOF, cut-cell for solids, boundary conditions, parallel implementation, Oct-tree adaptation, ...
- Gerris style for program flow (e.g. GfsVariable, GfsEvent, GfsSource, GfsFunction, GfsOutput,...)
- Object-oriented programming using only ANSI-C\*;

Learning curve is steep if you want to adapt Gerris for modest complex problems!

\* Object Oriented Programming with ANSI C, Axel-Tobias Schreiner, 1993



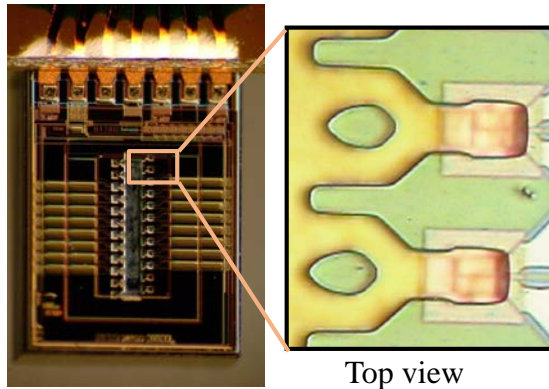
# Outline

- How do I get started with Gerris
- **Droplet formation in Inkjet process**
- Capillary flow in low-gravity
- Droplet-media interaction
- Future work

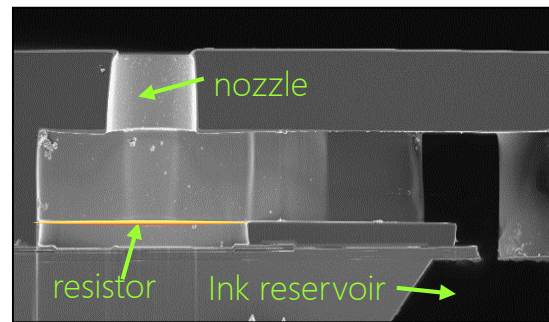


# Droplet formation in Inkjet process

## Drop-on-Demand (DOD) Thermal Inkjet (TIJ)

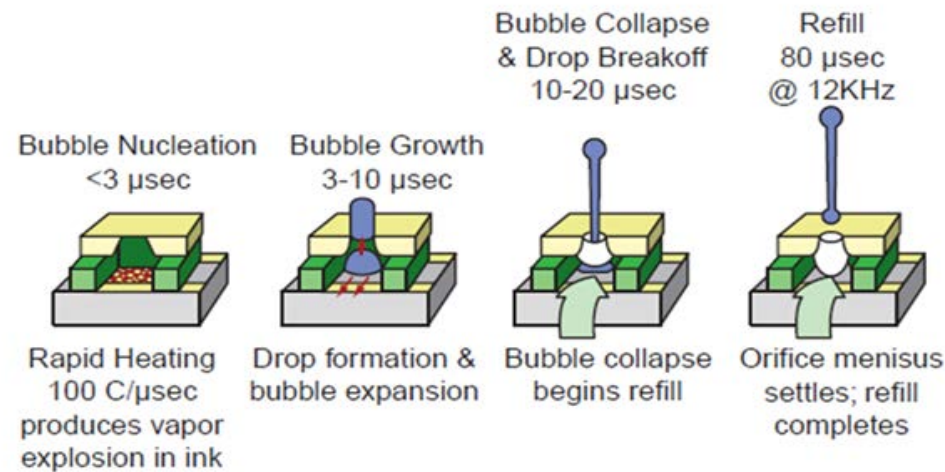


Top view

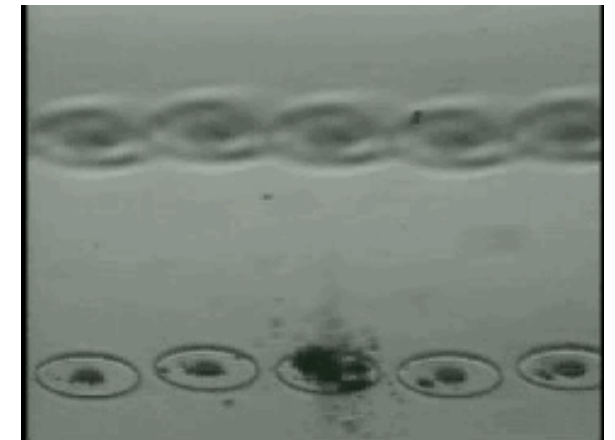


Cross-section

Schematic of a firing chamber structure



Droplet-ejection sequence in TIJ



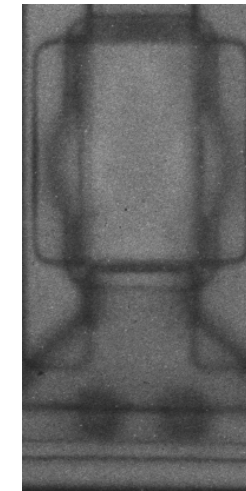
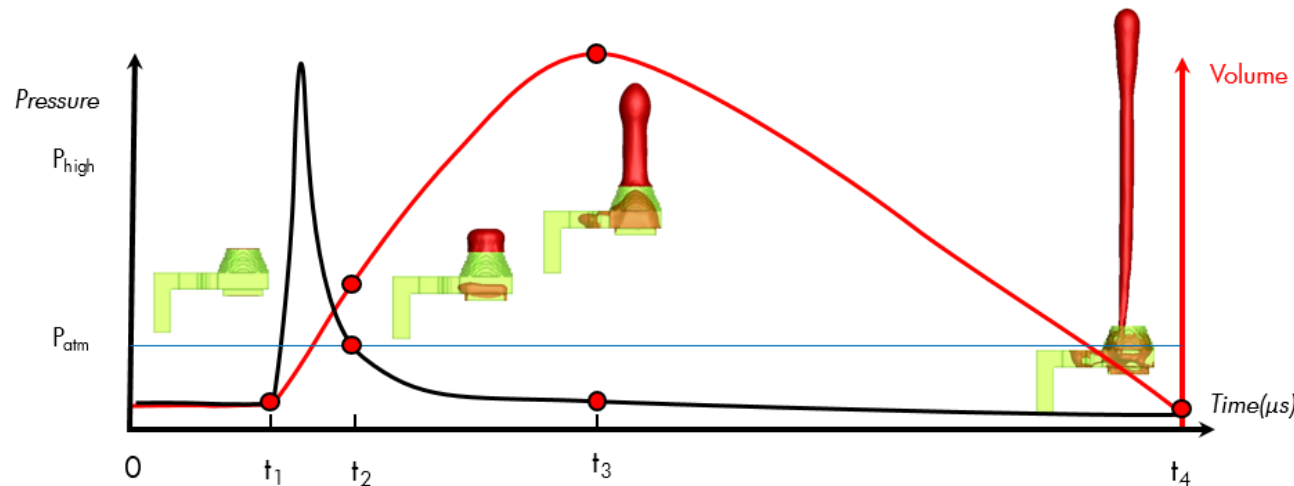
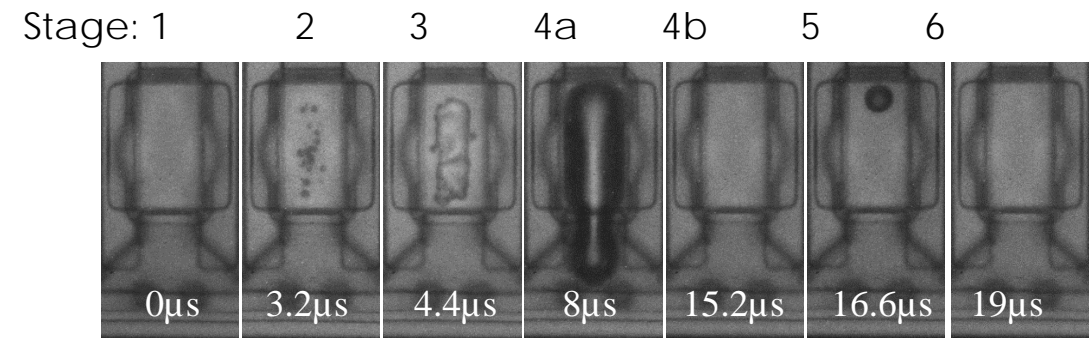
High-speed imaging of TIJ



# Droplet formation in Inkjet process

**TIJ boiling:** heat flux  $1-2 \times 10^9 \text{ W/m}^2$ . (Sun surface  $\sim 6.58 \times 10^7 \text{ W/m}^2$ )

1. Thin film heating
2. Boiling incipience (pre-nucleation)
3. Boiling
4. Vapor bubble expansion & collapse
5. Rebound
6. Vapor bubble disappears





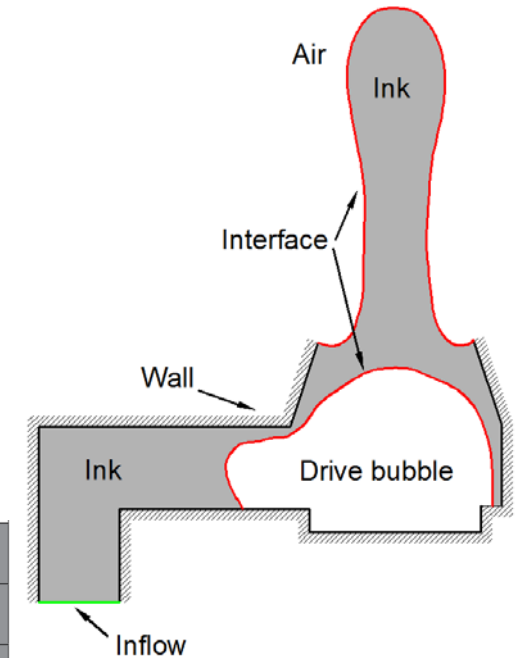
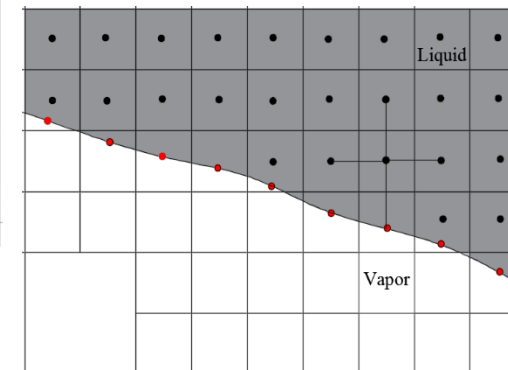
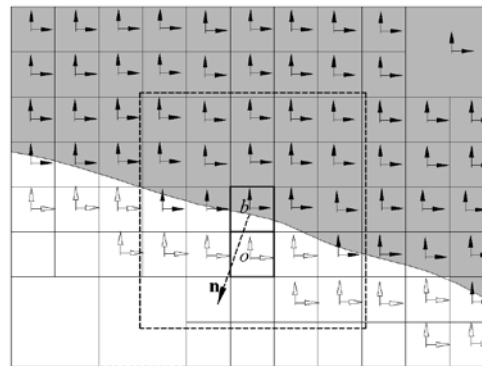
# Droplet formation in Inkjet process

## Drive bubble dynamics

- Assume that the adiabatic expansion and collapse of the drive bubble follow a polytropic process ( $pV^n = \text{constant}$ ).
- Bubble can split and merge due to geometry constrains.
- Velocity in empty cells adjacent to vapor-liquid interface is extrapolated for calculation the advection and viscous terms conveniently without the irregular computing stencils\*

$$\Gamma = \sum_{k=1}^N (\mathbf{u}_o + \mathbf{A} \cdot \mathbf{x} - \mathbf{u}_k)^2 + \lambda \mathbf{t} \cdot (\mathbf{A} + \mathbf{A}^T) \cdot \mathbf{n}$$

\*Popinet, S. and S. Zaleski, *Bubble collapse near a solid boundary: a numerical study of the influence of viscosity*. Journal of Fluid Mechanics, 2002. **464**: p. 137-163.



$$-p = -p_g + \sigma K - \mathbf{n} \cdot \boldsymbol{\tau} \cdot \mathbf{n}$$

$$\mathbf{t} \cdot \boldsymbol{\tau} \cdot \mathbf{n} = 0$$



# Droplet formation in Inkjet process

## Contact angle model

Capillary force plays an important role in the refill of the firing chamber.

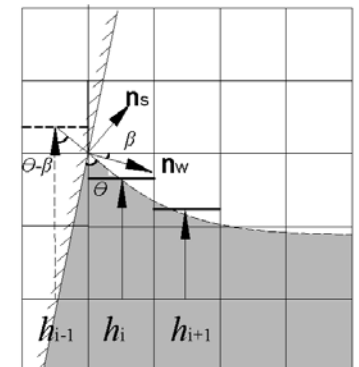
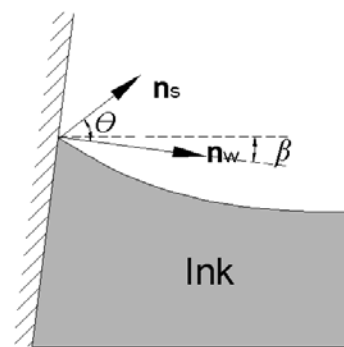
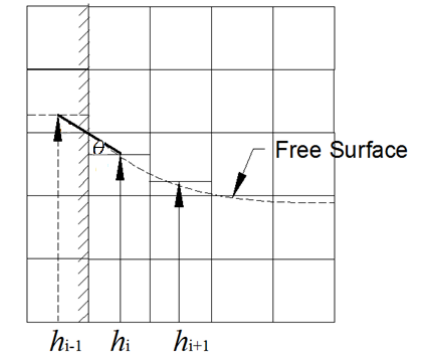
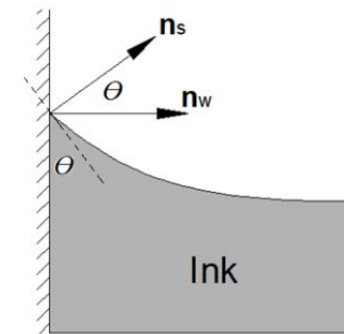
A fictitious height function in the solid wall can be calculated by

$$h_{i-1} = h_i + \frac{\Delta}{\tan \theta}$$

When the normal direction  $\mathbf{n}_w$  of the wall is not aligned with the Cartesian directions.

$$h_{i-1} = h_i + \frac{\Delta}{\tan(\theta - \beta)}$$

Calculation of 3D case is more complicated than that for 2D case, especially when  $\mathbf{n}_w$  is not aligned with the Cartesian direction.



# Droplet formation in Inkjet process

## Gerris implementation

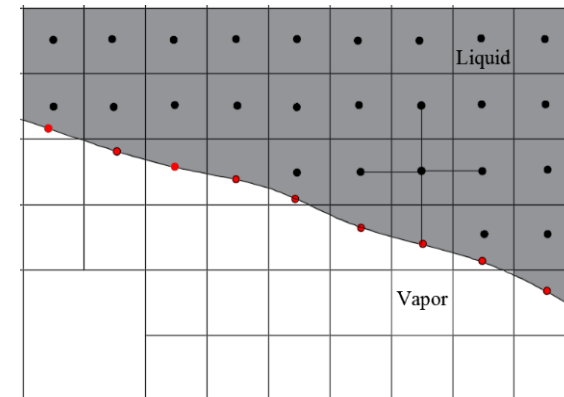
- Create a new event class '**drive\_bubble\_event**' to handle the drive bubble dynamics (e.g. initialize the drive bubble parameters, flag drive bubble, calculate drive bubble volume, pressure, track the bubble state, etc.).
- Create a new method '**gfs\_diffusion\_bubl**' to handle the solution of provisional velocity (in fractional-step projection method for NS equations) involving vapor-liquid interface.

$$\rho^{n+1/2} \left[ \frac{\mathbf{u}^* - \mathbf{u}^n}{\Delta t} + (\mathbf{u}^{n+1/2} \cdot \nabla) \mathbf{u}^{n+1/2} \right] = \nabla \cdot \left[ \mu^{n+1/2} \left( (2 - \beta) \mathbf{D}^n + \beta \mathbf{D}^* \right) \right] + (\sigma \kappa \delta_s \mathbf{n})^{n+1/2}$$

- Create a new method '**gfs\_poisson\_solve\_bubl**' to handle the solution of the Poisson equation involving vapor-liquid interface.

$$\nabla \cdot \left[ \frac{\Delta t}{\rho^{n+1/2}} \nabla p^{n+1/2} \right] = \nabla \cdot \mathbf{u}^*$$

- Implement a 3D version of **GfsVariableTracerVOFHeight** in vof.c
- Create a new class '**surface\_angle\_bc\_class**' to specify the contact angle for solid walls and implement relevant curvature calculation adjustment in vof.c.
- Create a few new methods in GerrisOutput (e.g. statistics of droplets, interface segments, tecplot output, etc.)
- Clean bugs especially when a complex solid geometry present.



# Droplet formation in Inkjet process

## Gerris implementation

```

4 3 GfsSimulation GfsBox GfsGEdge {} {
  Global {
    #define LEVEL 7
    #define GRAVITY 980
    #define MU_L 1.3e-2
    #define MU_G 1.8e-4
    #define RHO_L 1.
    #define RHO_G 1.e-3
    #define var(T,min,max) (CLAMP(T,0,1)*(max - min)
+ min)
    #define rho(T) var(T, RHO_G/RHO_L, 1.)
    #define mu(T) var(T, MU_G/MU_L, 1.)
    #define Z_t 22e-4
    #define Noz_t -10e-4
    #define PA 1.01e6
    #define P_back 9950
  // back pressure
    static double pressure_refill (double x, double y,
double z, double P) {
    if (x < -27e-4 && y <= -48e-4 && fabs(z) < Z_t)
return -P_back;
    return P;
  }
  // vof boundary
    static double vof_bc (double x, double y, double z) {
    if (y < -48e-4 && fabs(z) <= Z_t) return 1.;
    else return -1.;
  }
}

```

```

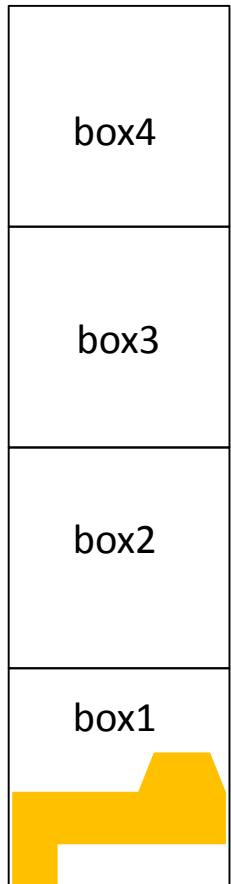
// initial drive bubble
    static double drive_bubble (double x, double y, double z)
{ if (fabs(z) >= Z_t)
    return -1.;
  else if (y < Noz_t && !(x > -11e-4 && y < -37.9e-4))
    return 1.;
  else
    return -1.; }
}
GfsTime { end = 40.e-6 }
GfsRefine 1
GfsRefineSolid LEVEL
GfsSolid solid.gts
VariableTracerVOFHeight {} T
Variable T0
InitFractionT0 (vof_bc(x, y, z))
VariableFiltered T1 T 3
InitFraction {} T (drive_bubble(x, y, z))
PhysicalParams {L = 100.e-4 alpha = 1/rho(T1)/RHO_L }
SourceViscosity MU_L*mu(T1)
VariableCurvature K T Kmax
SourceTension T 50 K
AdaptFunction { irstart = 1 istep = 1 } {cmax = 0.1 maxlevel =
LEVEL cfactor = 2 } (T > 0 && T < 1)
GModule drive_bubble
DriveBubble {} T {direction = 2 crit_factor = 8. p_high =
8e6 p_floor = 3.e5 pa = PA}
SurfaceAngleBc T 40

```

```

EventBalance {istep=1} 0.1
OutputBalance {istep = 1} balance
GfsOutputSimulation { step = .25e-6} file-inkjet-vof-%ld.gfs
GfsOutputSimulation { step = .25e-6 } tecplot-%ld.dat
{variables= U,V,W,P,Tsolid=0 format = Tecplot}
GfsOutputTiming { istep = 20 } stdout
}
GfsBox {bottom = Boundary {
  BcDirichlet T T0 BcDirichlet P pressure_refill(x,y,z,P)
  BcNeumann V 0 BcDirichlet U 0 BcDirichlet W 0 }
  right = BoundaryOutflow left = BoundaryOutflow
  front = BoundaryOutflow back = BoundaryOutflow
}
GfsBox { pid = 1
  right = BoundaryOutflow left = BoundaryOutflow
  front = BoundaryOutflow back = BoundaryOutflow
}
GfsBox { pid = 2
  right = BoundaryOutflow left = BoundaryOutflow
  front = BoundaryOutflow back = BoundaryOutflow
}
GfsBox { pid = 3
  right = BoundaryOutflow left = BoundaryOutflow
  front = BoundaryOutflow back = BoundaryOutflow
  top = BoundaryOutflow
}
1 2 top
2 3 top
3 4 top

```

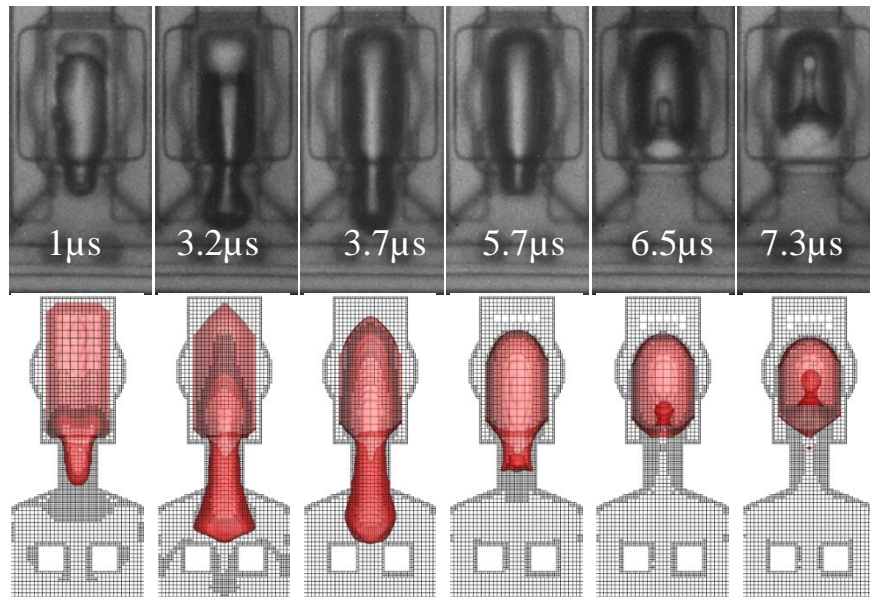
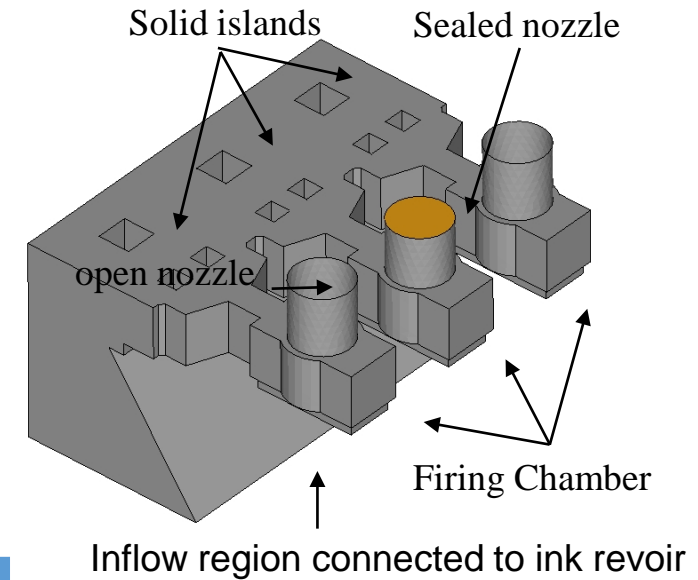


# Droplet formation in Inkjet process

## Simulation Examples\*

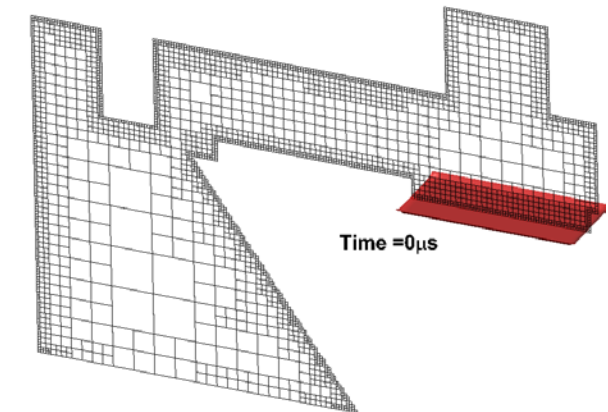
### Vapor bubble behavior in TIJ firing chamber

Voltage 26V, pulse width 3 $\mu$ s, water at 25°C, Domain size is 130  $\mu$ m $\times$ 130  $\mu$ m $\times$ 130  $\mu$ m, the finest level L= 8,  $\Delta_{min}$ =0.75  $\mu$ m.



### Input parameters

Variable	value
Viscosity $\mu$	0.001 kg/ms
Surface tension $\sigma$	0.07 kg/s <sup>2</sup>
Density $\rho$	1000 kg/m <sup>3</sup>



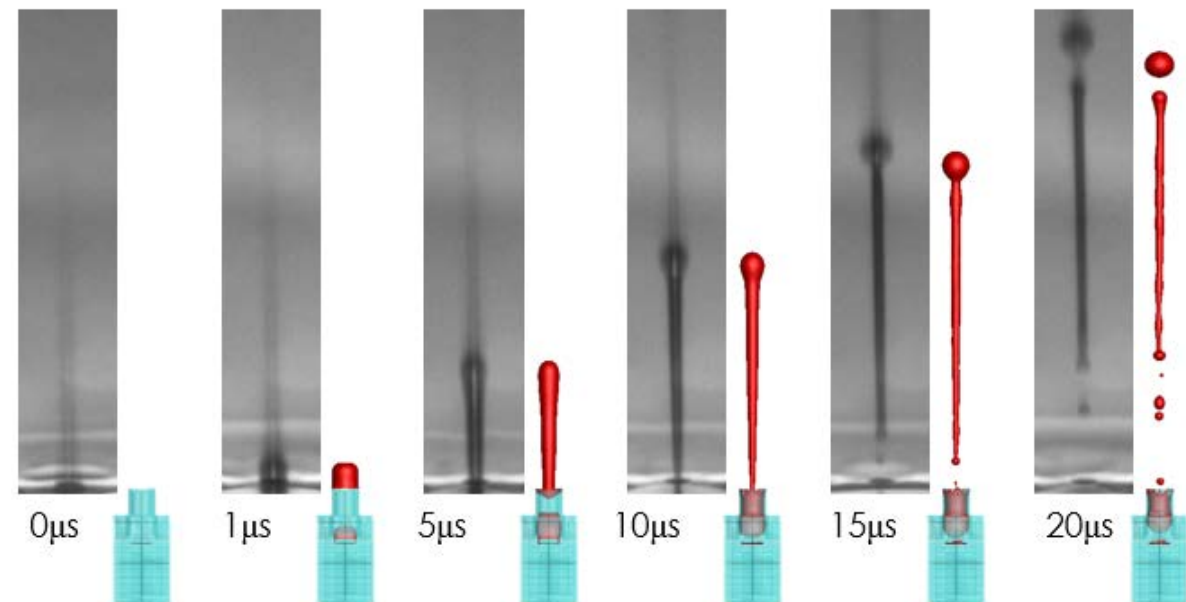
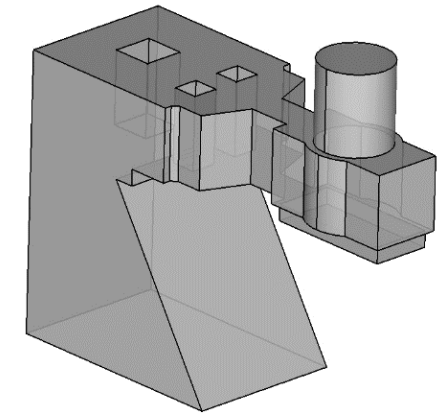
# Droplet formation in Inkjet process

## Simulation Examples\* droplet-ejection simulation

- Domain size:  $125\mu\text{m} \times 125\mu\text{m} \times 625\mu\text{m}$ ,  $L_{\text{max}}: 8$ ,  $\Delta_{\text{min}}: 0.5\mu\text{m}$ . The mesh is adaptive to the interface curvature and local velocity gradient.
- Summary of results

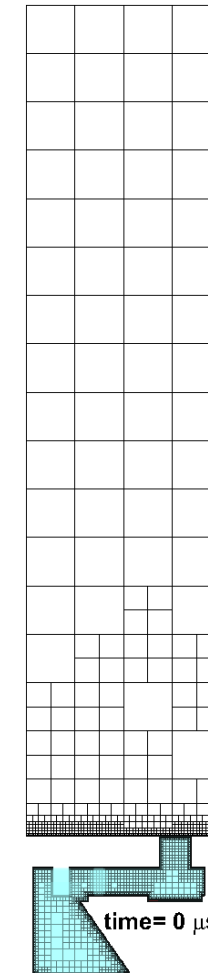
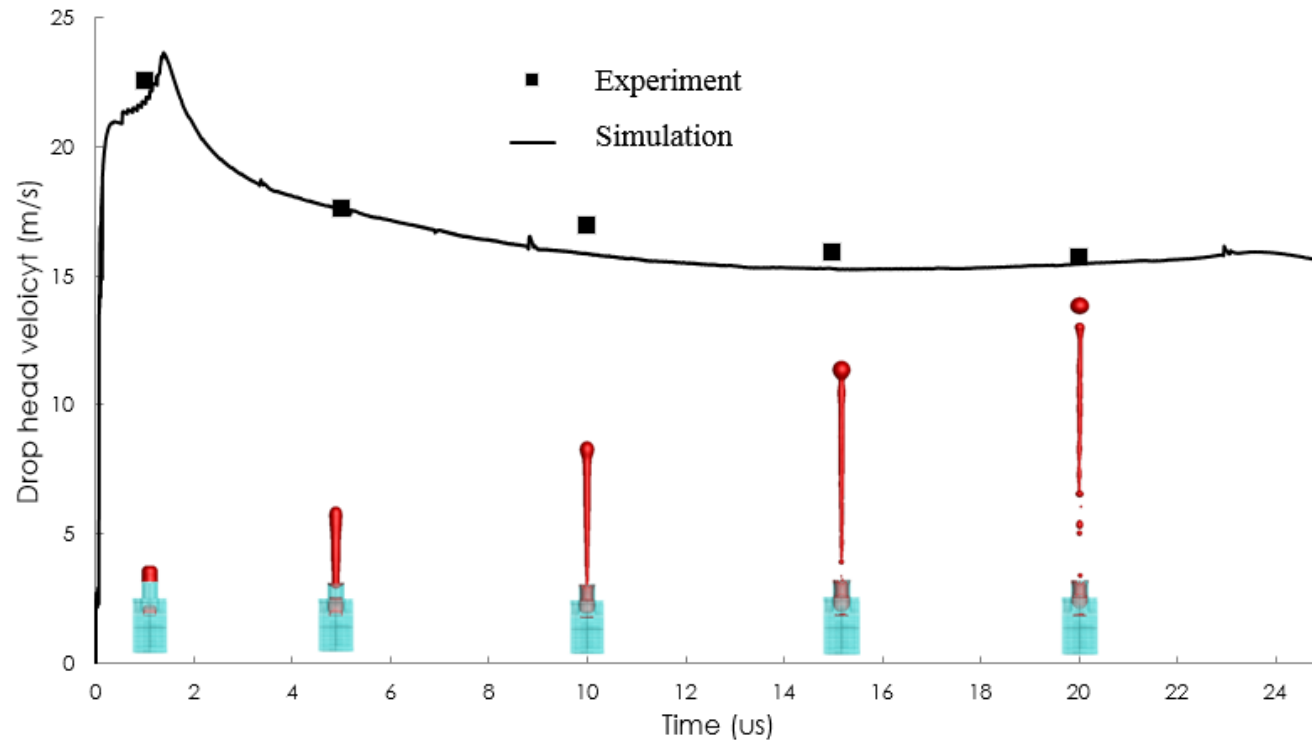
	Experiment	Simulation
Droplet weight (ng)	9.8	10.1
Droplet speed (m/s)	15.4	15.3
Refill frequency (kHz)	20	16

Variable	value
Viscosity $\gamma$	$0.011 \text{ cm}^2/\text{s}$
Surface tension $\sigma$	$40 \text{ dyn/cm}$
Density $\rho$	$1.0 \text{ g/cm}^3$
Contact Angle	$45^\circ$



# Droplet formation in Inkjet process

## Simulation Examples\* droplet-ejection simulation



Side view



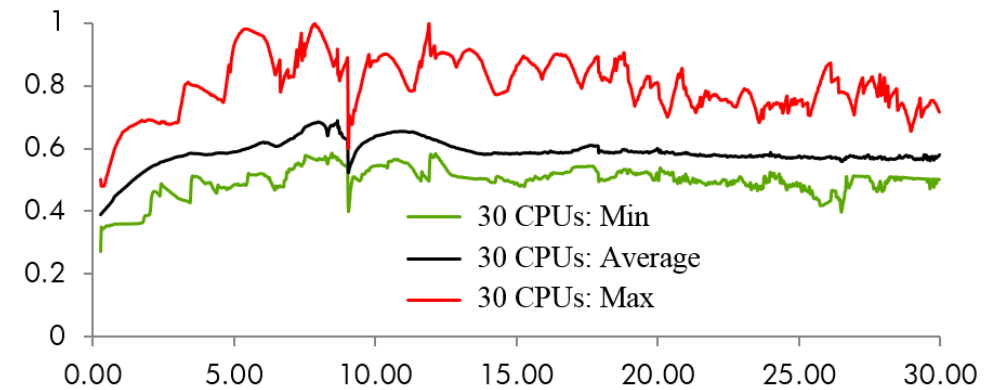
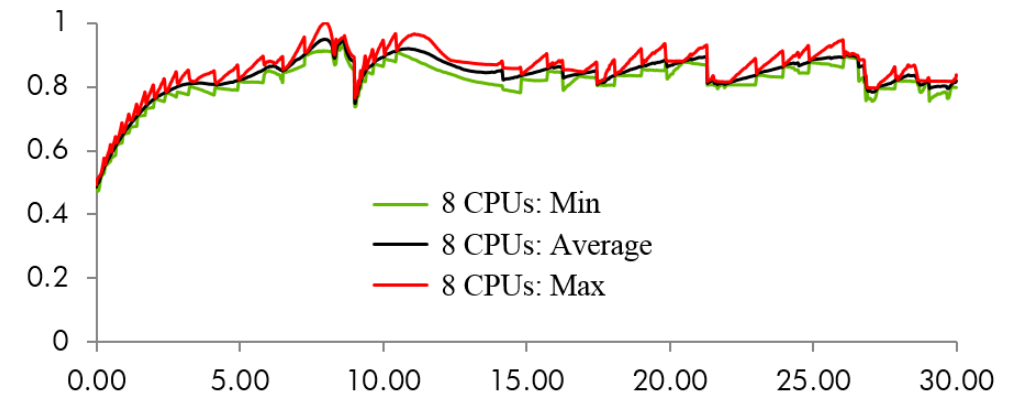
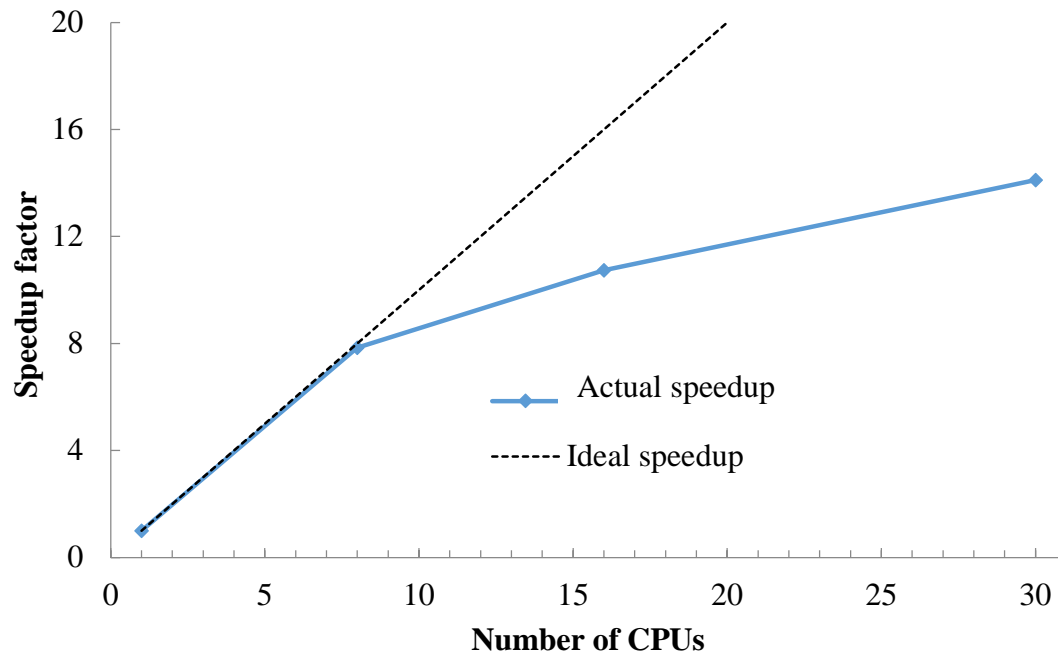
Front view



# Droplet formation in Inkjet process

## Simulation Examples\* droplet-ejection simulation

Parallel performance



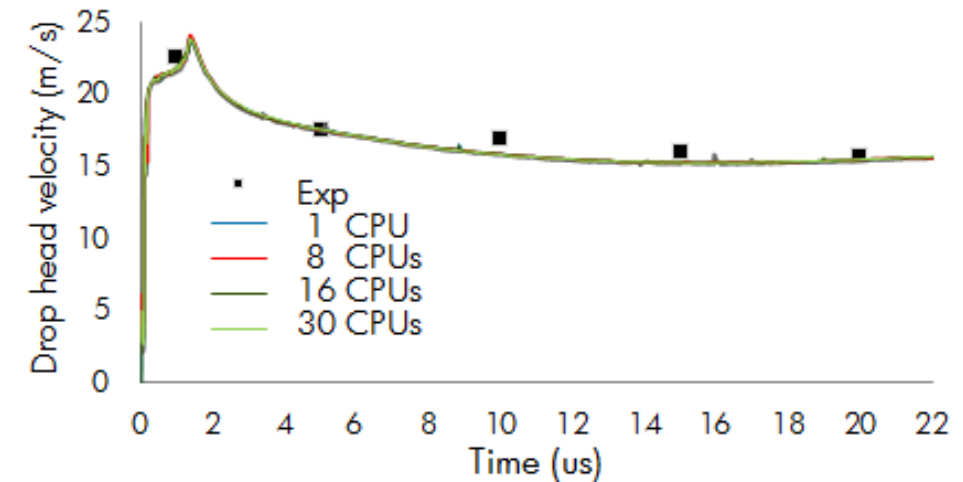
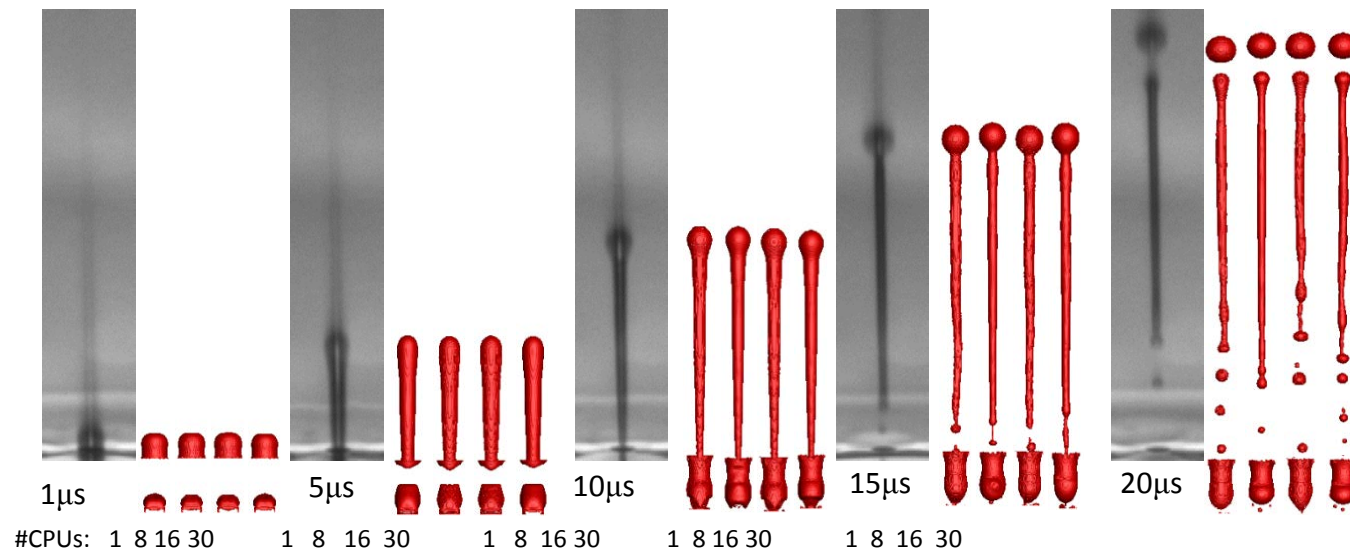


# Droplet formation in Inkjet process

## Simulation Examples\*

### droplet-ejection simulation

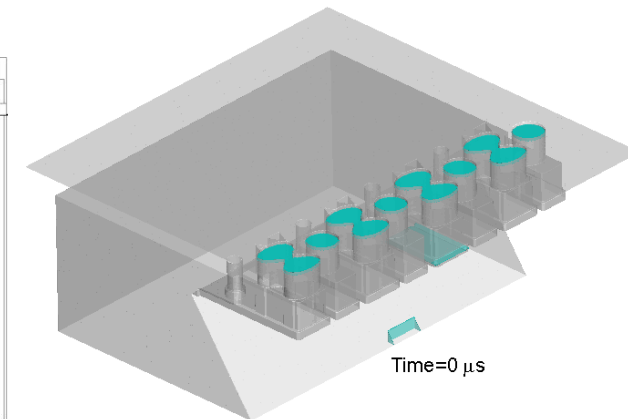
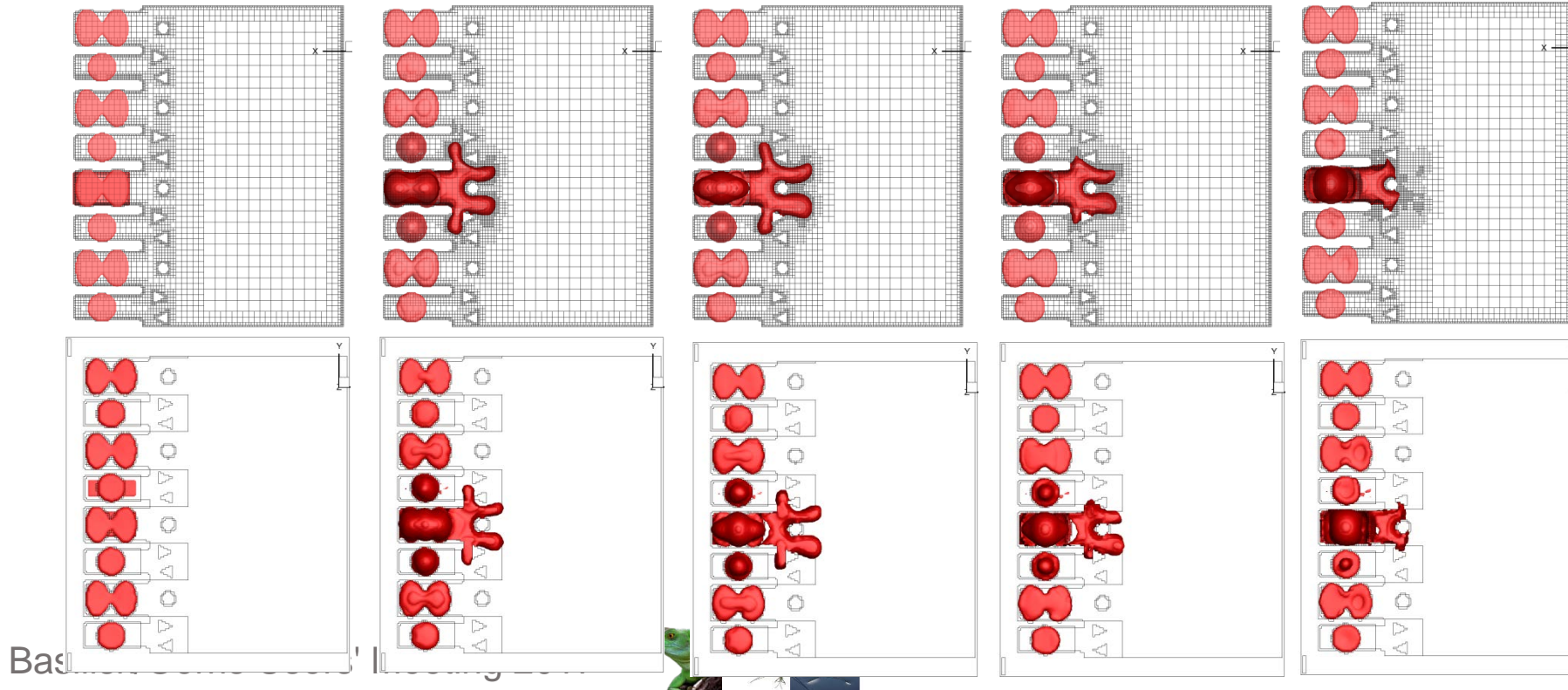
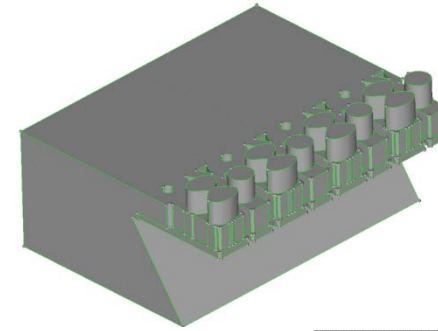
Effect of parallel computation on solution



# Droplet formation in Inkjet process

## Simulation Examples droplet-ejection simulation

Multi-nozzle case



# Droplet formation in Inkjet process

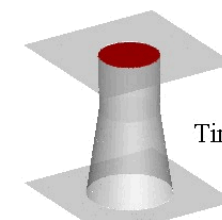
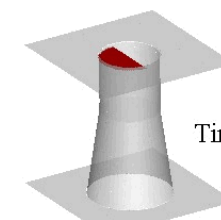
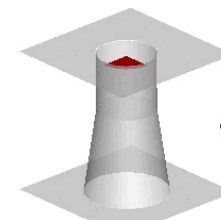
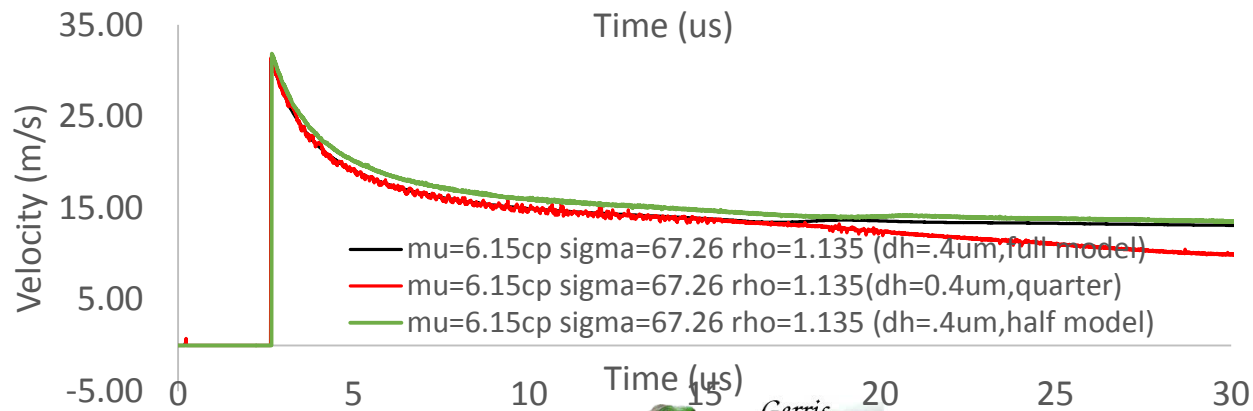
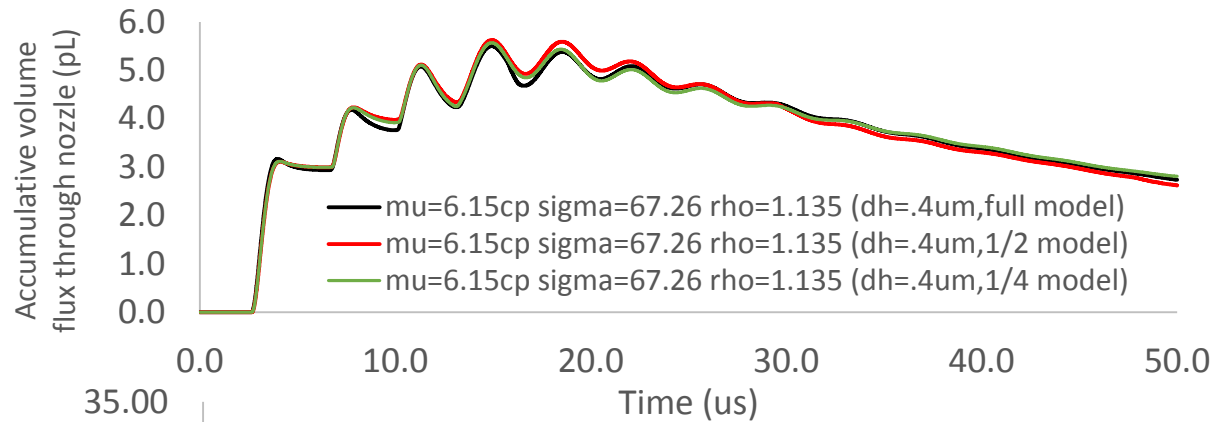
1/4 model

1/2 model

full model

## Simulation Examples

full-model, 1/4-model, and 1/2-model

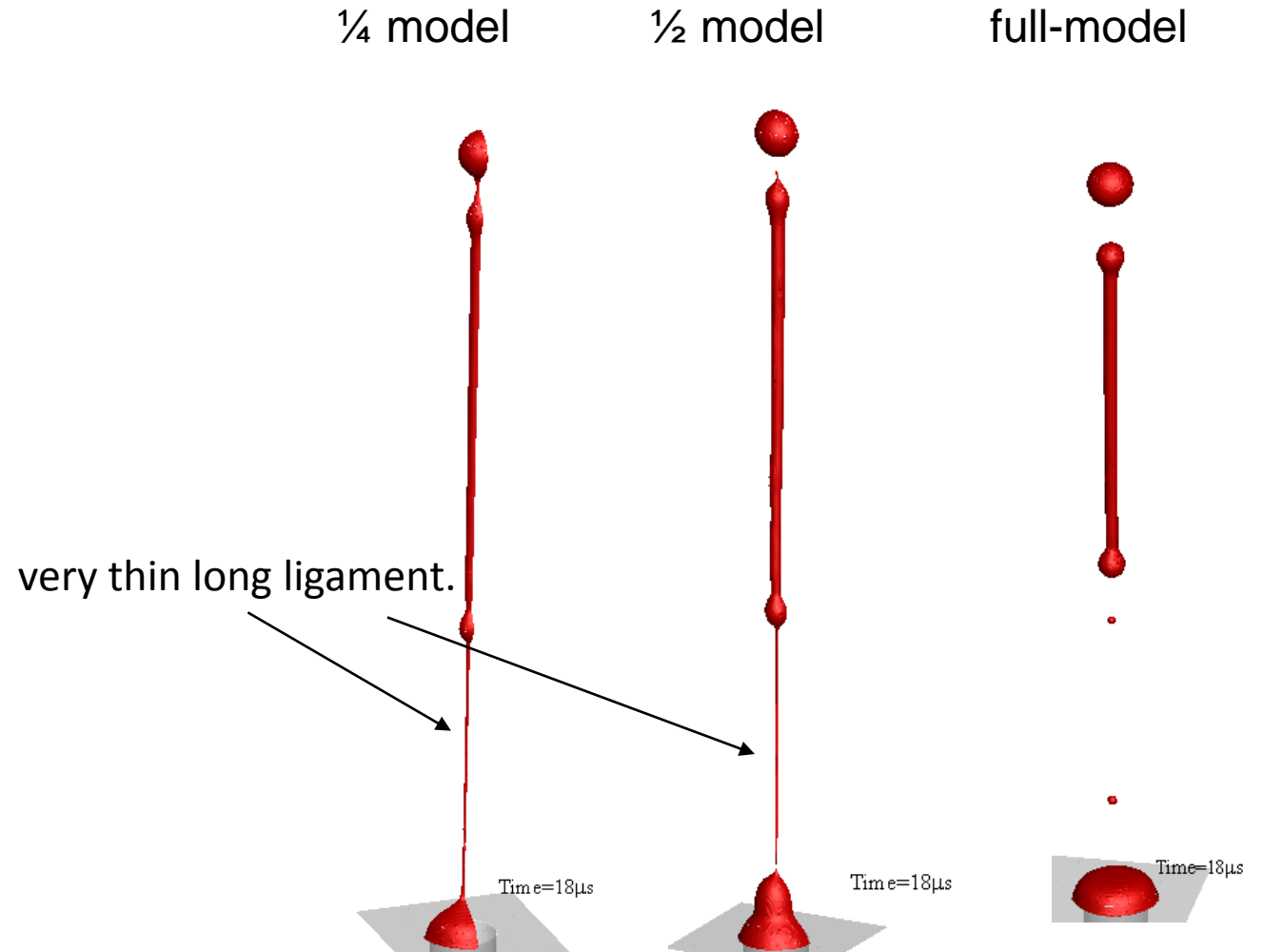


# Droplet formation in Inkjet process

## Simulation Examples

For drop velocity and volume, all three models give very close results.

Both  $\frac{1}{2}$ - and  $\frac{1}{4}$ -models predict a very thin and long ligament after the end blob in the tail, whereas full-model predicts two very small satellite droplets.



# Outline

- How do I get started with Gerris
- Droplet formation in Inkjet process
- **Capillary flow in low-gravity**
- Droplet-media interaction
- Future work



# Capillary flow in low-gravity

## Puddle jump\*



2.1-s drop tower facility at Portland State University ( $g \leq 2 \times 10^{-4} g_0$ ).

Vol=2 mL



30mL



95mL



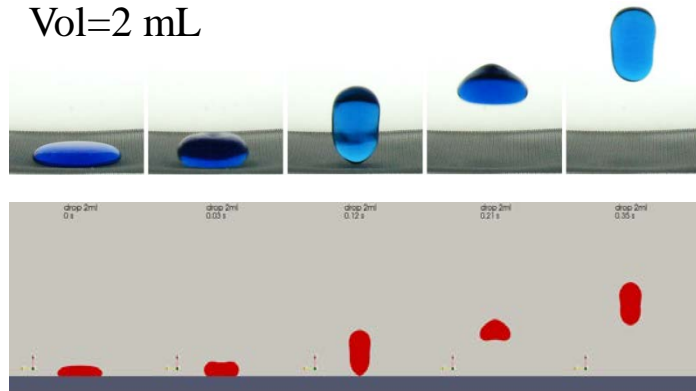
A puddle jumps from superhydrophobic surface in low-g condition.



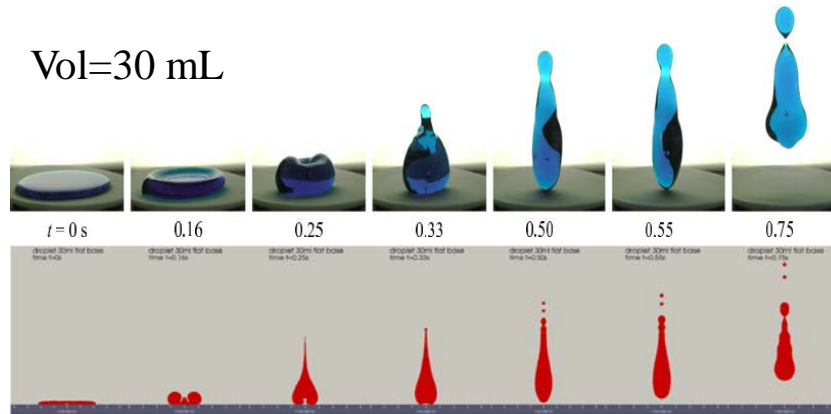
# Capillary flow in low-gravity

## Puddle jump\*

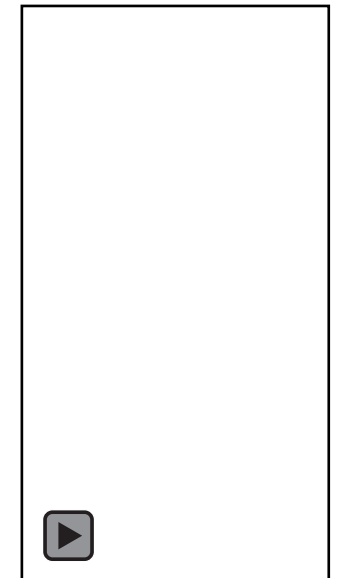
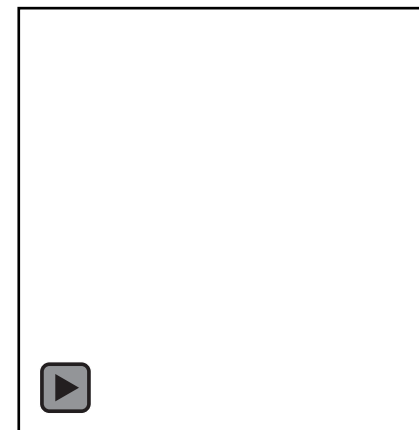
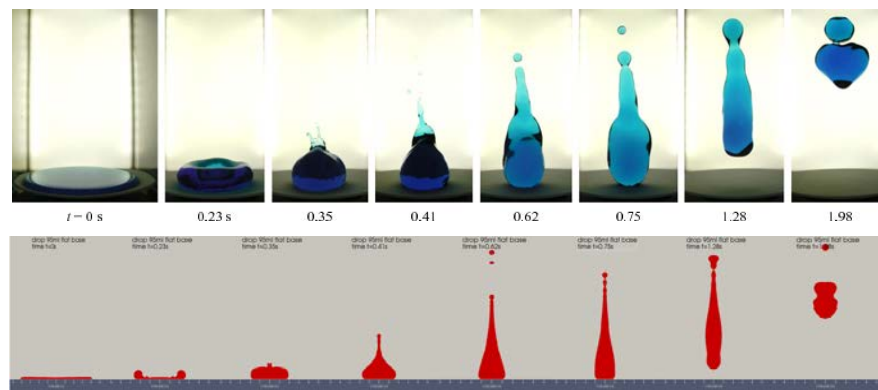
Vol=2 mL



Vol=30 mL

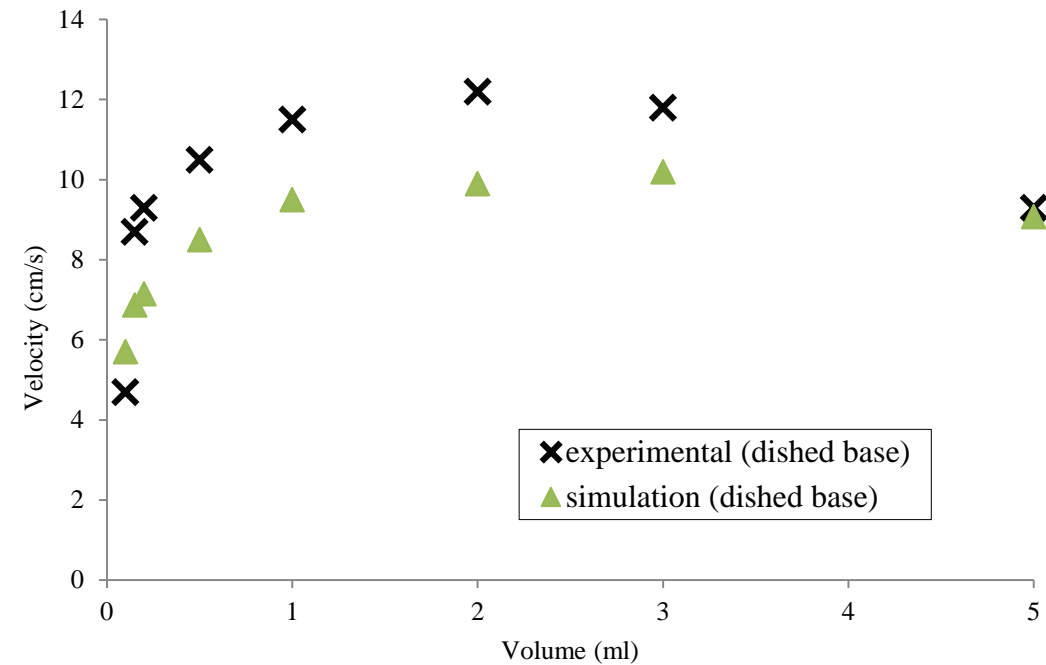
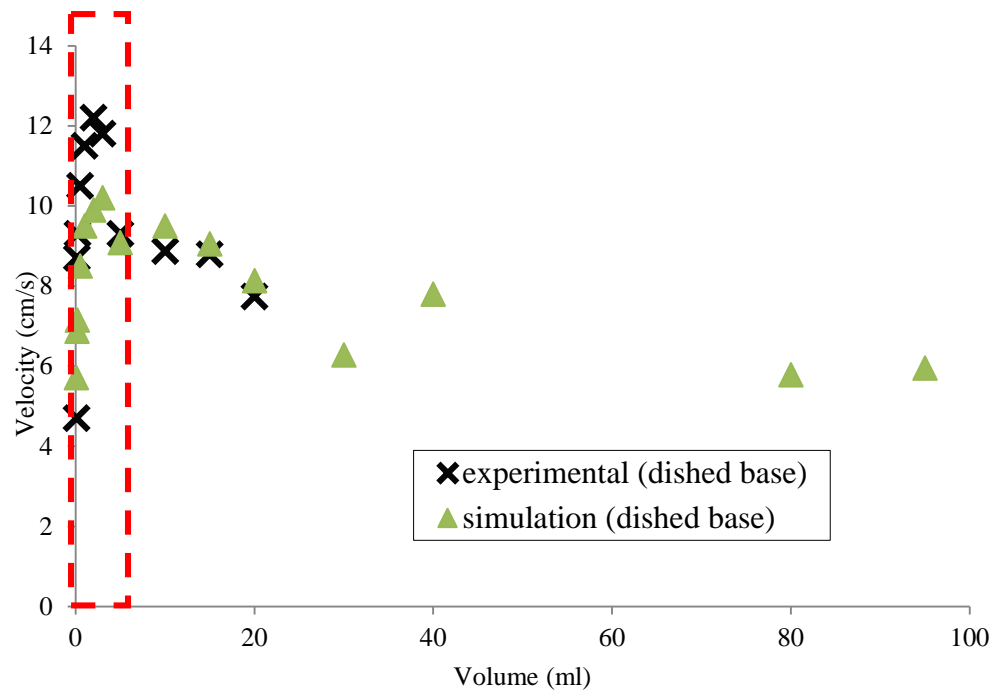


Vol=95 mL



# Capillary flow in low-gravity

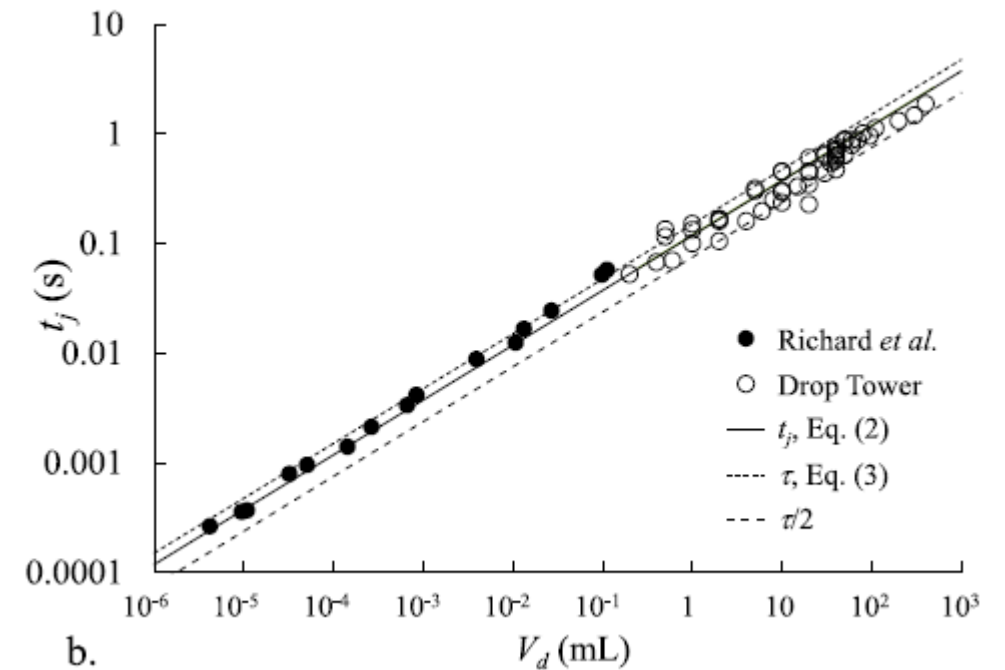
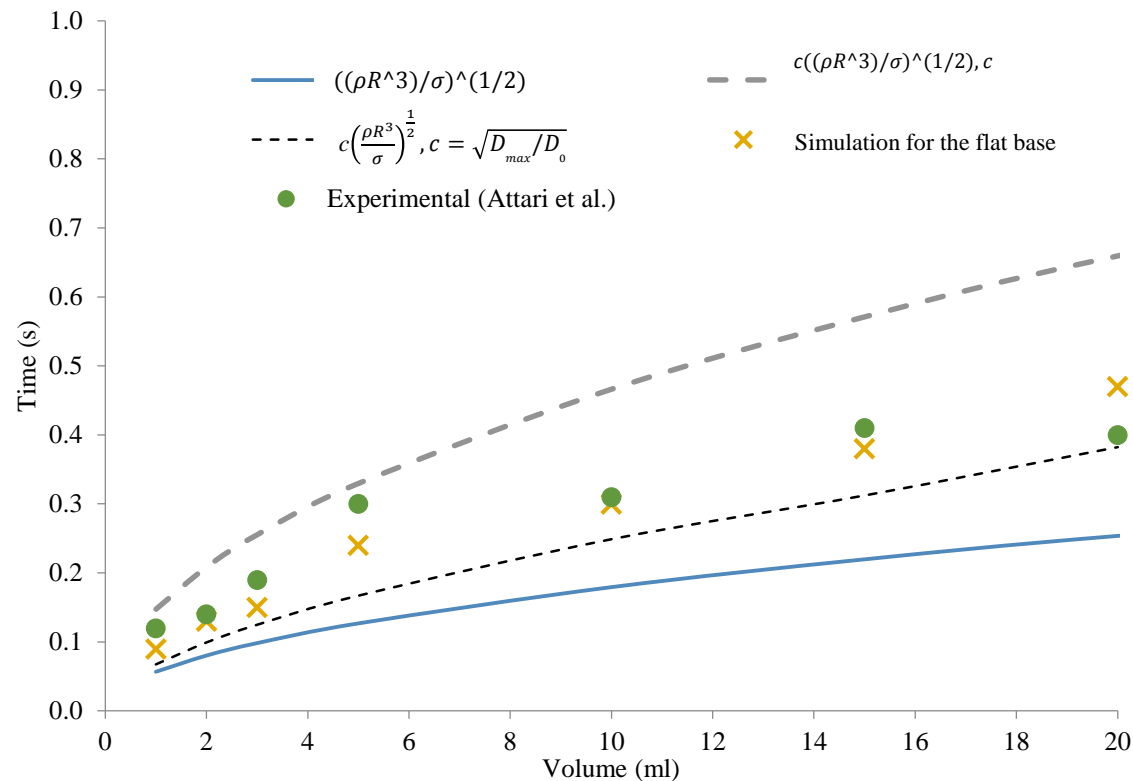
## Puddle jump





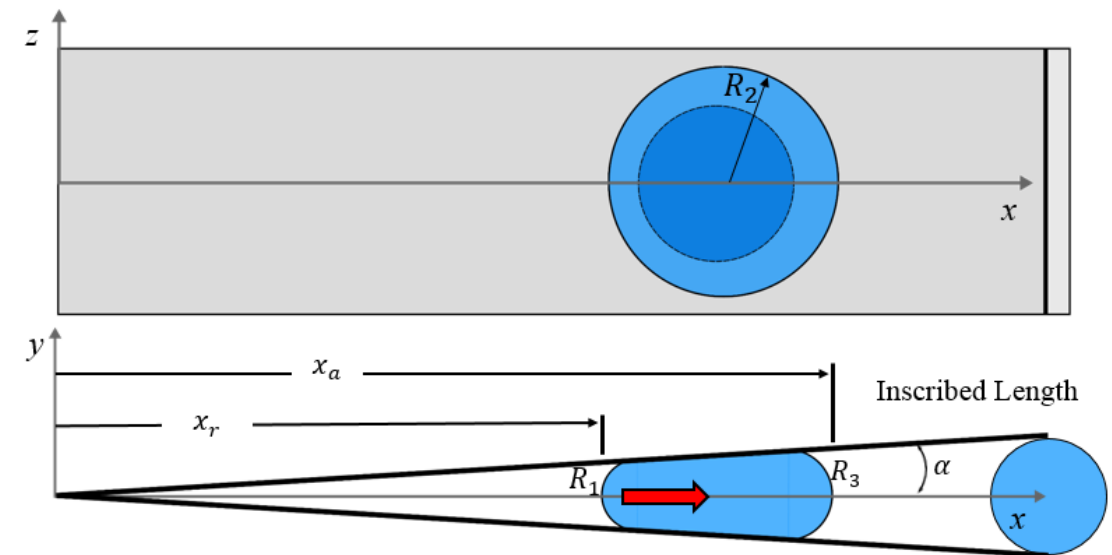
# Capillary flow in low-gravity

**Puddle jump**  $\tau_c = c \left( \frac{\rho R^3}{\sigma} \right)^{\frac{1}{2}}$



# Capillary flow in low-gravity

## Capillary migration in super-hydrophobic wedges\*



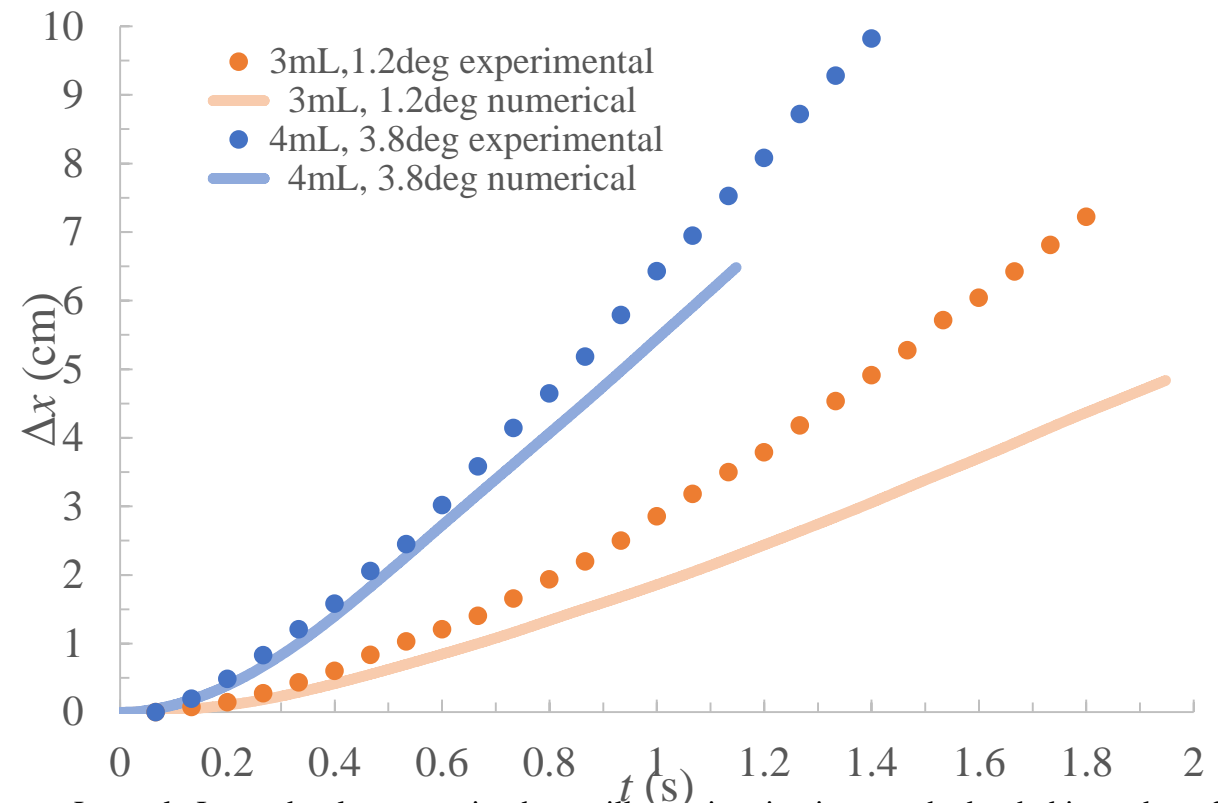
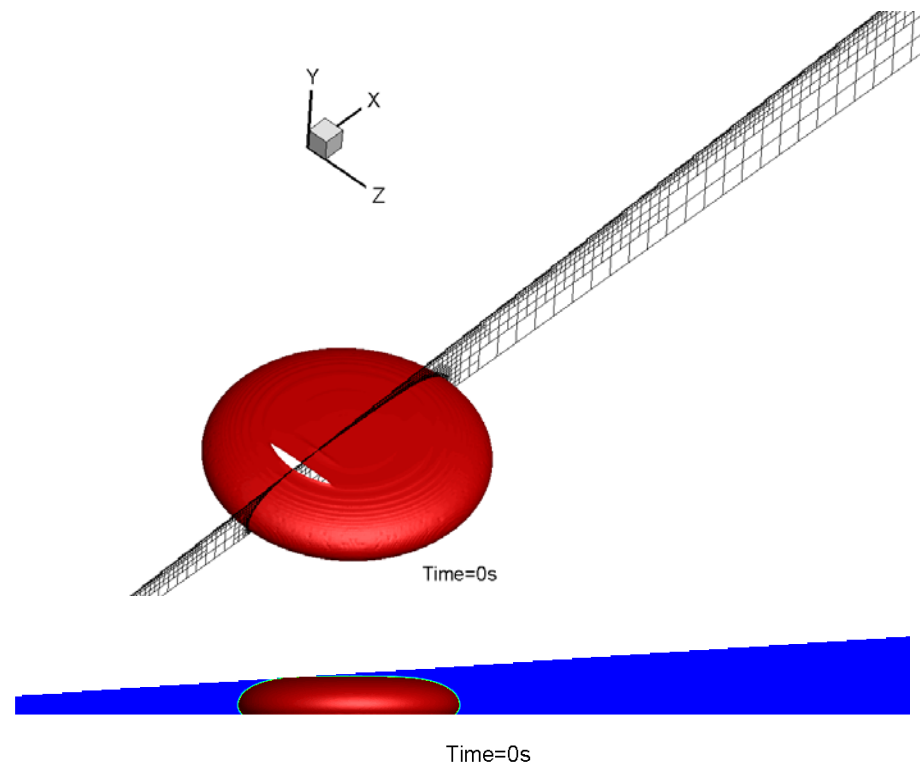
$$\Delta P_{net} \approx \sigma \left( \frac{1}{R_1} - \frac{1}{R_3} \right) \quad U \approx \left( \frac{\sigma g}{\rho} \right)^{1/4} \left[ -2 \cos \theta + 2 \left( \frac{\pi H}{V} \right)^{1/2} - 6^{2/3} \left( \frac{\pi H}{V} \right)^{1/3} \right]^{1/2}$$

$$t_{jw} \approx \left( \frac{3V}{4\pi} \right)^{1/3} \left( \frac{\rho}{\sigma g} \right)^{1/4} \frac{1}{-2 \cos \theta \cdot \sin \alpha}$$

# Capillary flow in low-gravity

## Capillary migration in super-hydrophobic wedges\*

4ml  $\alpha=3.8^\circ$



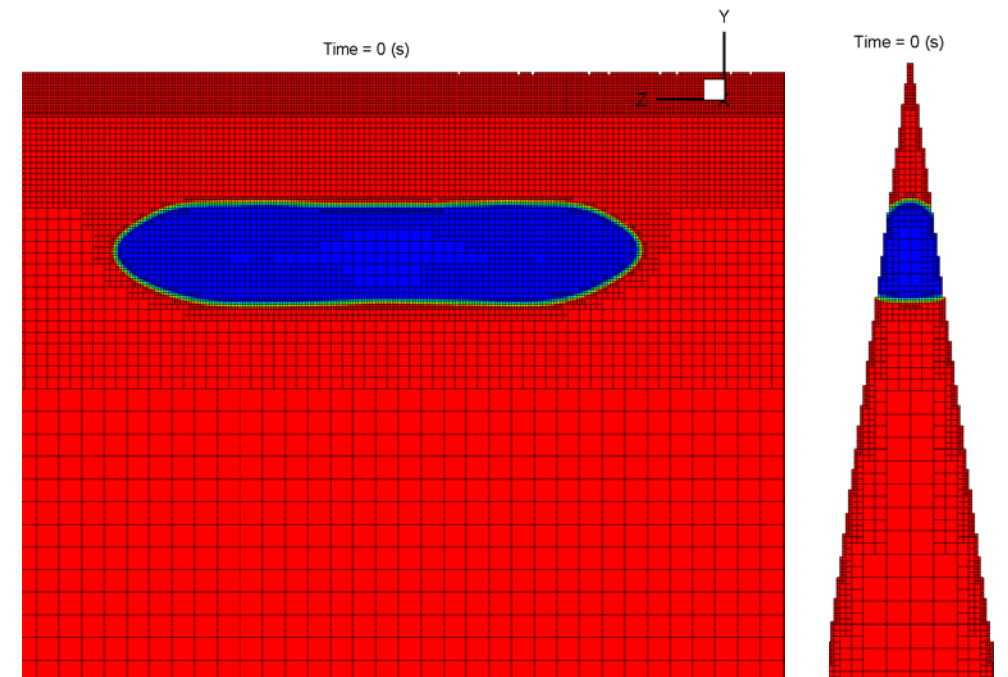
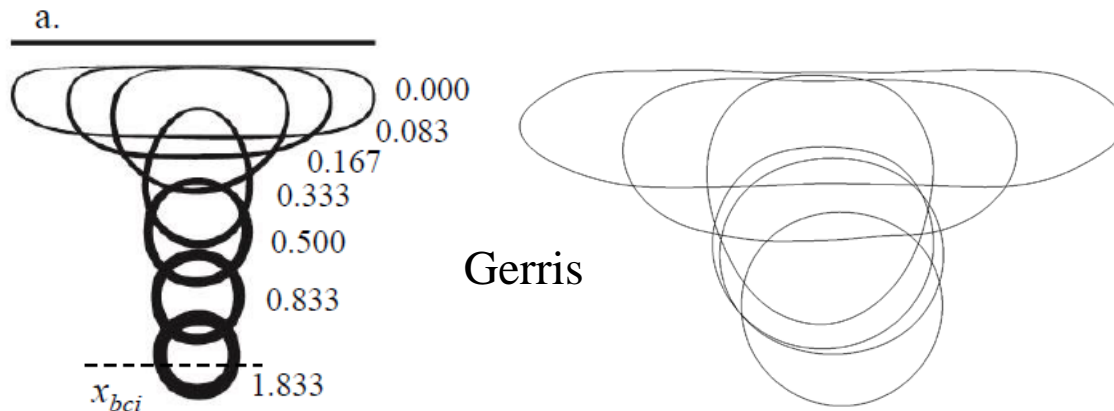
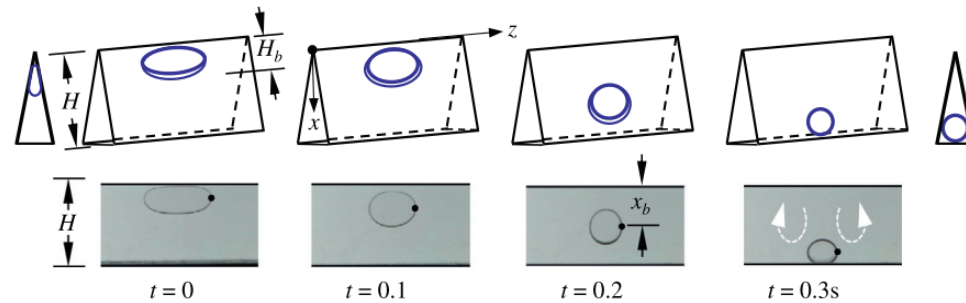
\*Torres, L., et al., Large droplet generation by capillary migration in super-hydrophobic wedges, 33rd Annual Meeting of the American Society for Gravitational and Space Research, ID306, Seattle, Oct. 25-28, 2017.



# Capillary flow in low-gravity

## Capillary migration in super-hydrophobic wedges\*

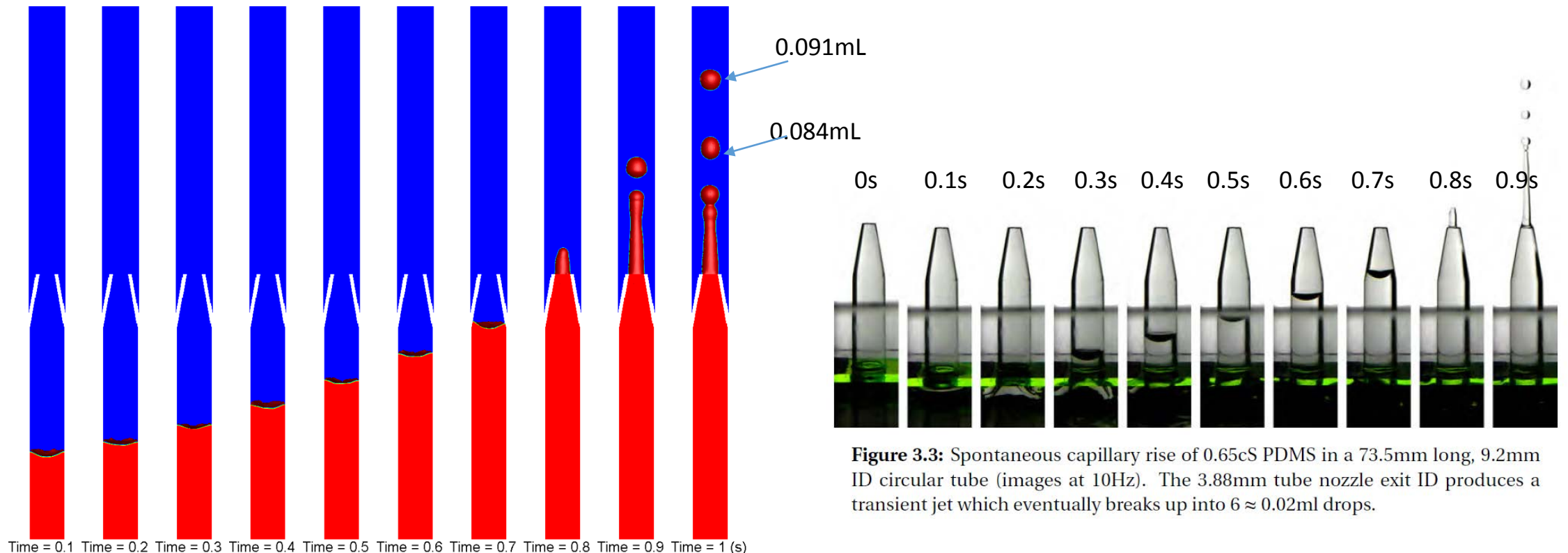
Jensen *et al.* 2014



\*Weislogel., et al., Capillary channel flow EU2-02 on the international space station: an experimental investigation of passive bubble separations in an open capillary channel, NASA/TM-20150218720.

# Capillary flow in low-gravity

## Auto-ejection\*



**Figure 3.3:** Spontaneous capillary rise of 0.65cS PDMS in a 73.5mm long, 9.2mm ID circular tube (images at 10Hz). The 3.88mm tube nozzle exit ID produces a transient jet which eventually breaks up into 6  $\approx$  0.02ml drops.

\*Wollman, A. and M. Weislogel, *New investigations in capillary fluidics using a drop tower*. Experiments in Fluids, 2013. **54**(4): p. 1499.



# Outline

- How do I get started with Gerris
- Droplet formation in Inkjet process
- Capillary flow in low-gravity
- **Droplet-media interaction**
- Future work

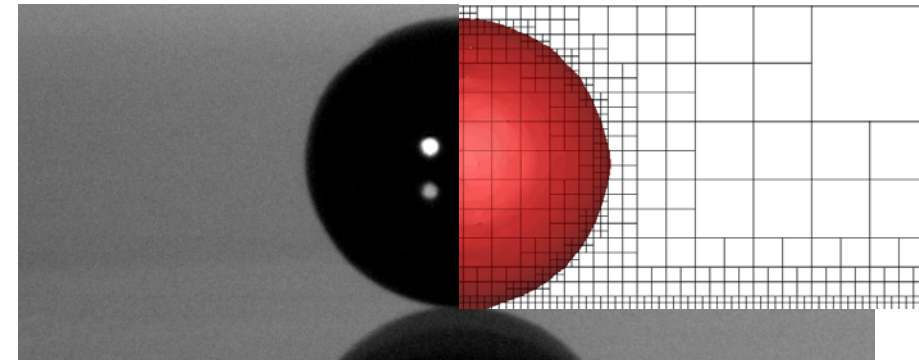
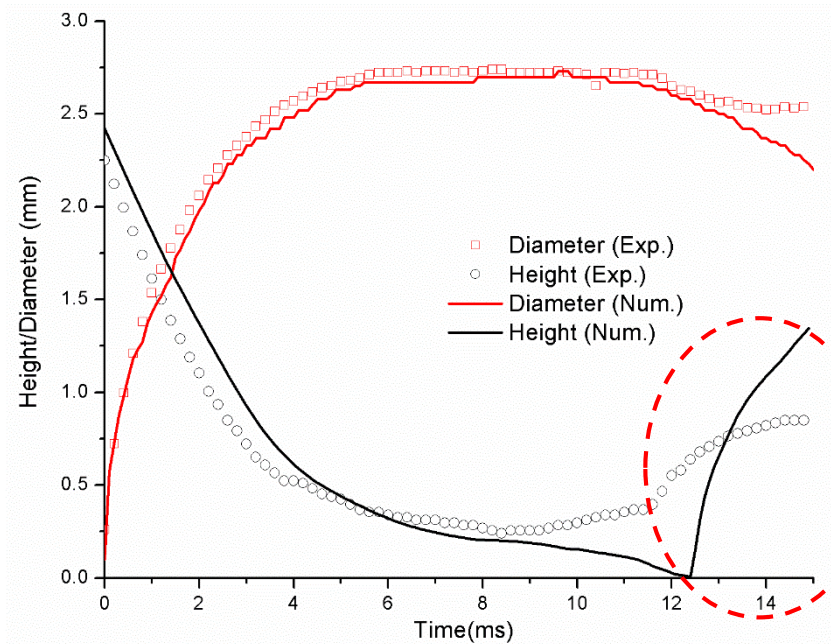


# Droplet-media interaction

## Droplet impact on glass surface\*

### Ink droplet

$U_0=0.57\text{m/s}$  ( $We=27$ )

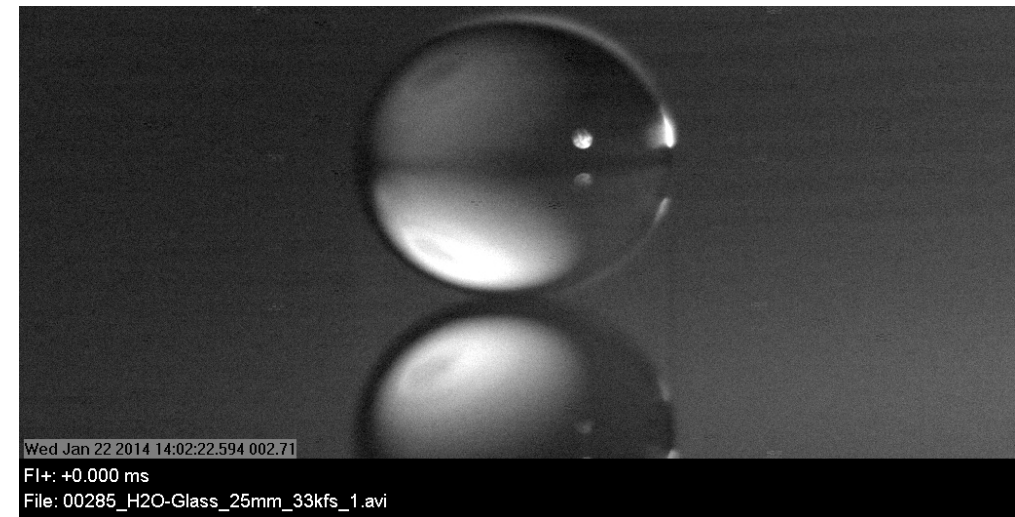
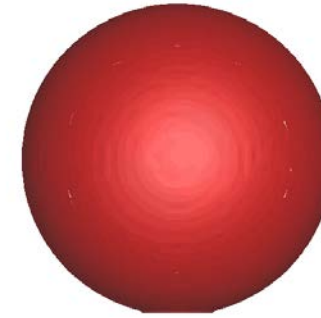
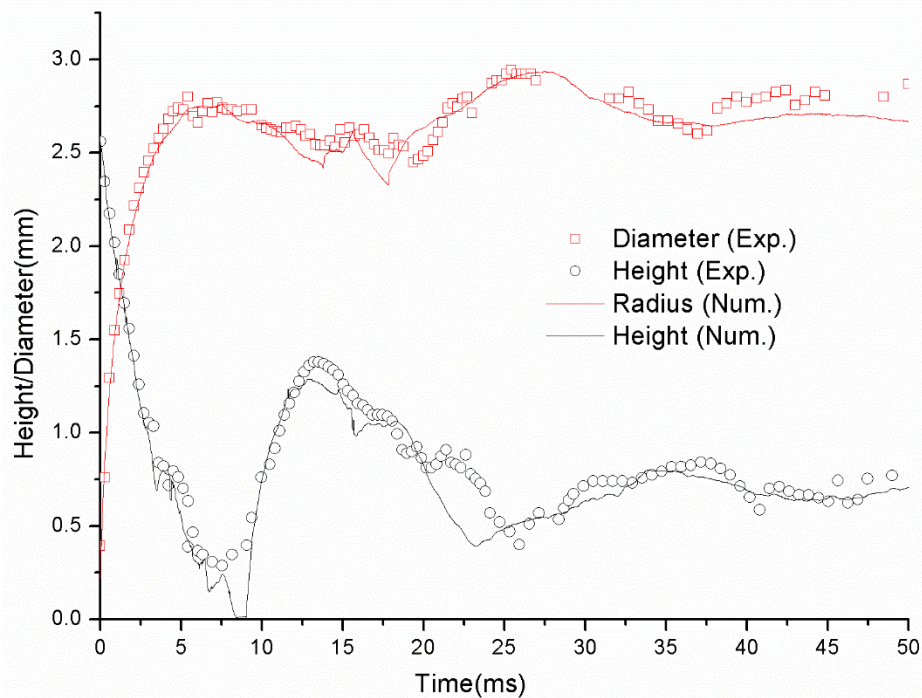


Simulation predicts much higher rebound. Dynamic surface tension plays an important role.



# Droplet-media interaction

## Droplet impact on glass surface\* Water droplet



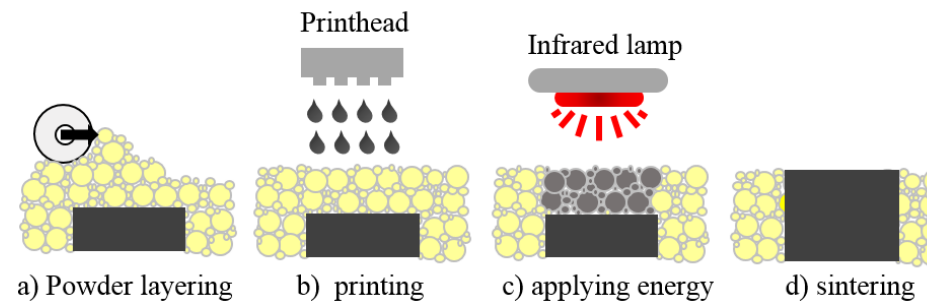


# Droplet-media interaction

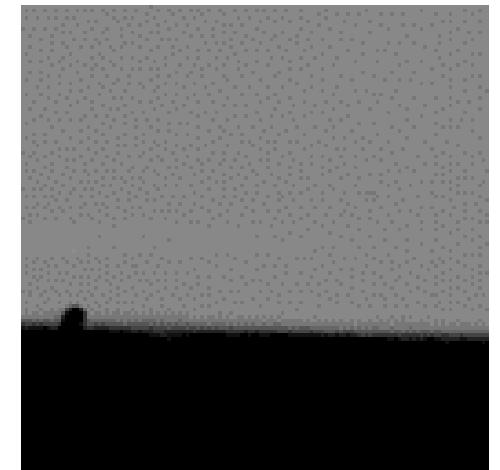
## Droplet impact on powders



High-speed sintering 3D printing machine



HSS 3D printing process: (a) powder is deposited on the build area by a roller; (b) A radiation absorbent ink is printed on desired area of the powder layer; (c) An infrared radiation source scans the entire build area; (d) The powder area masked by the ink is sintered and the entire process is repeated until the part is completed.



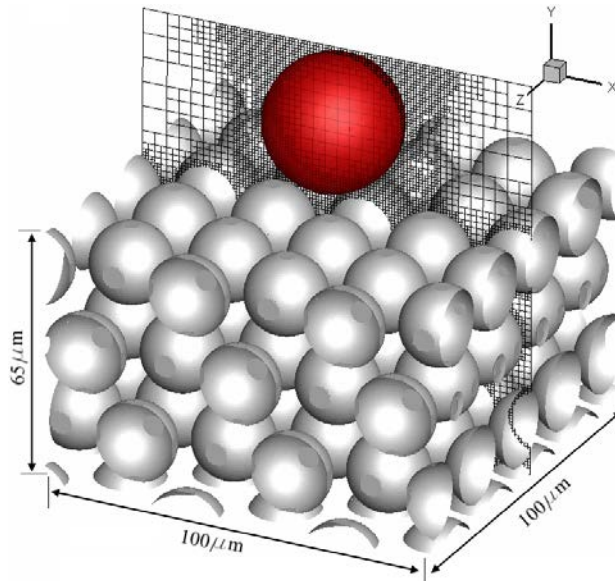
Drop impact on loose powder



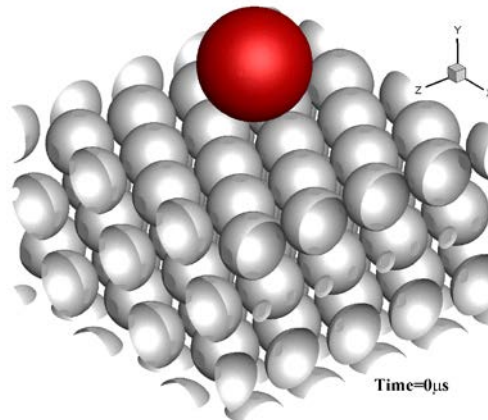
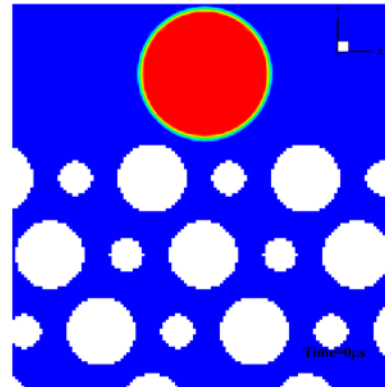
# Droplet-media interaction

## Droplet impact on powders\*

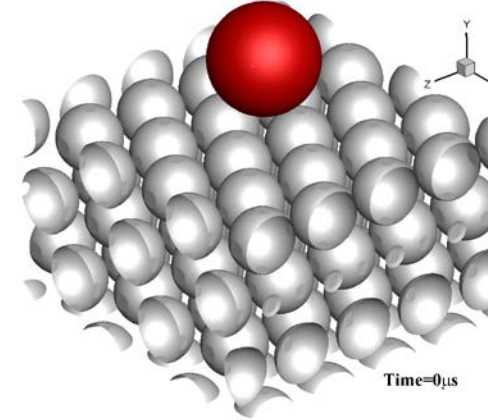
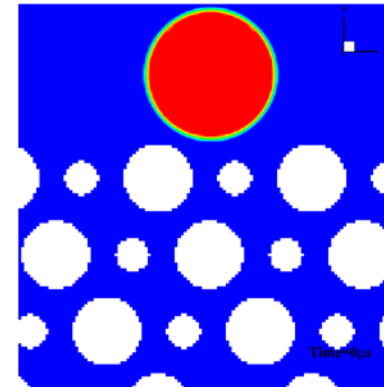
- impact velocities  $U_0=1\text{m/s}$ ,  $U_0=5\text{m/s}$ ,  $U_0=10\text{m/s}$ .
- Powder pack density is 0.4869, particle diameter= $20\mu\text{m}$
- Ink droplet diameter  $36.68\mu\text{m}$



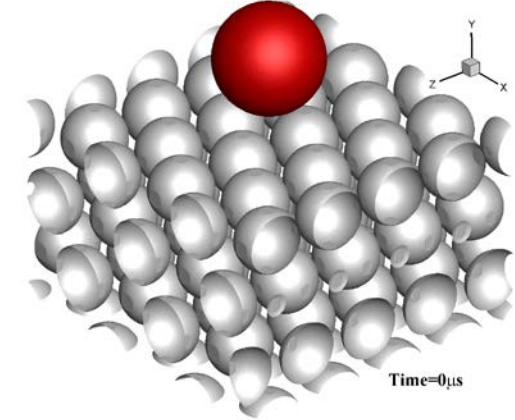
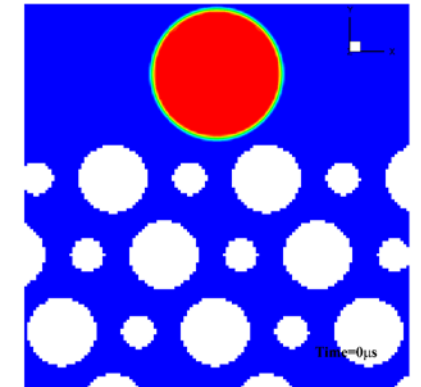
$U_0=1\text{m/s}$  ( $We=0.611$ )



$U_0=5\text{m/s}$  ( $We=15.3$ )

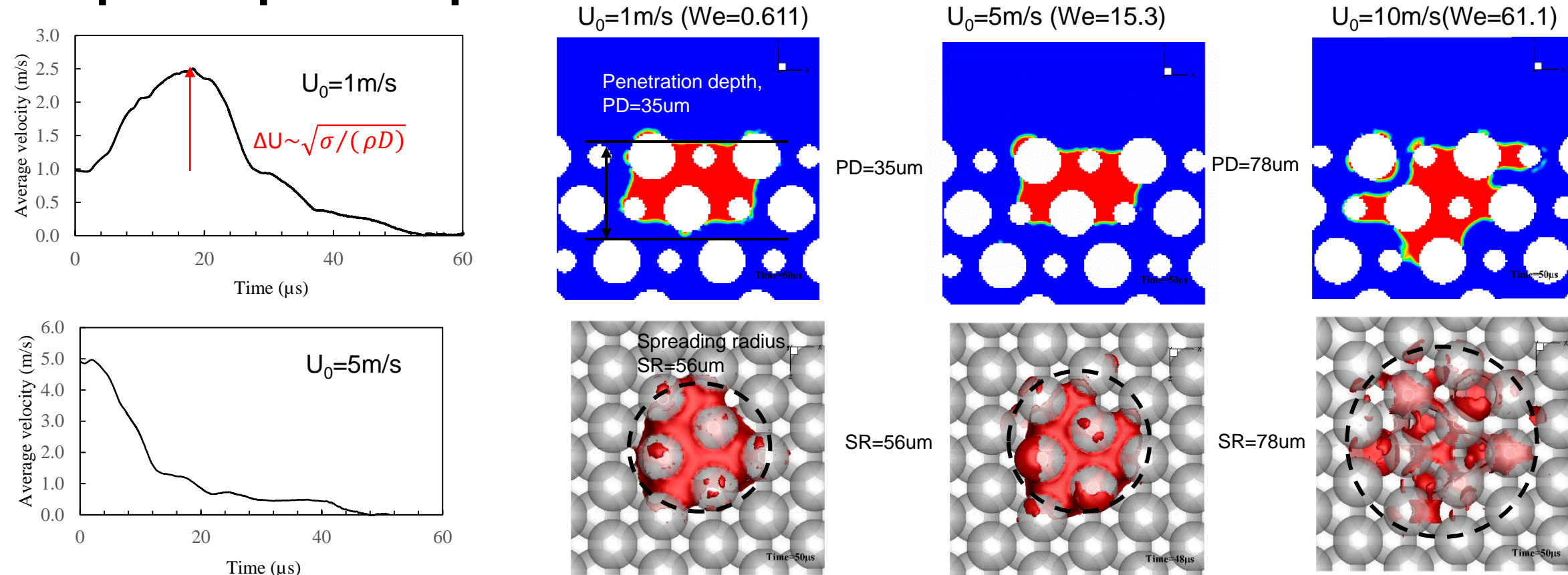


$U_0=10\text{m/s}$  ( $We=61.1$ )



# Droplet-media interaction

## Droplet impact on powders\*



# Droplet-media interaction

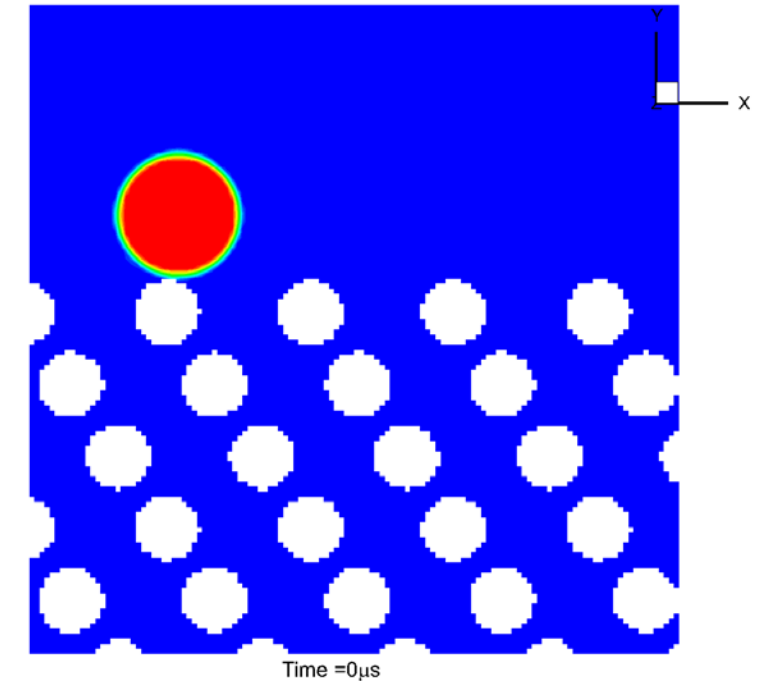
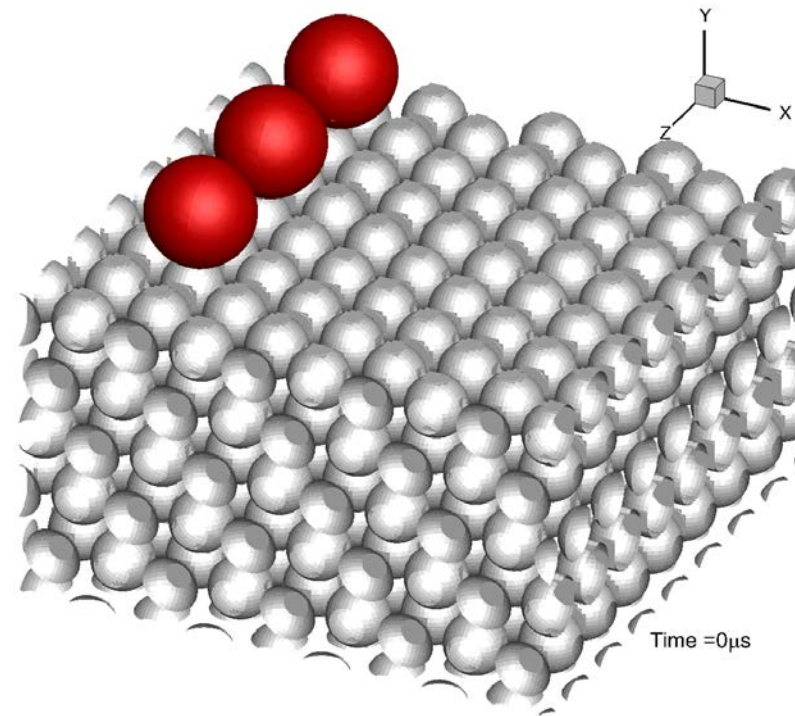
## Droplet impact on powders\*

Impact velocities  $U_0=5\text{m/s}$

Powder pack density is 0.4869

particle diameter= $20\mu\text{m}$

Ink droplet diameter  $36.68\mu\text{m}$

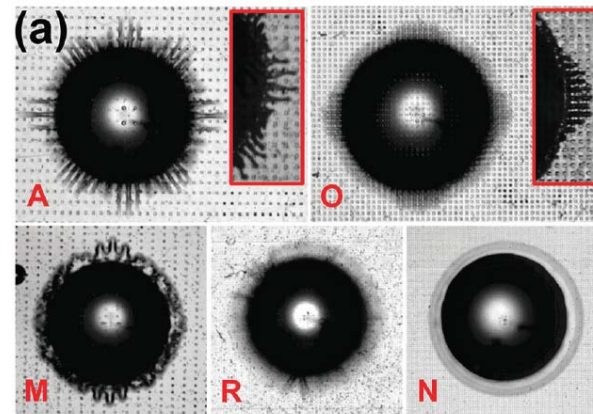


# Droplet-media interaction

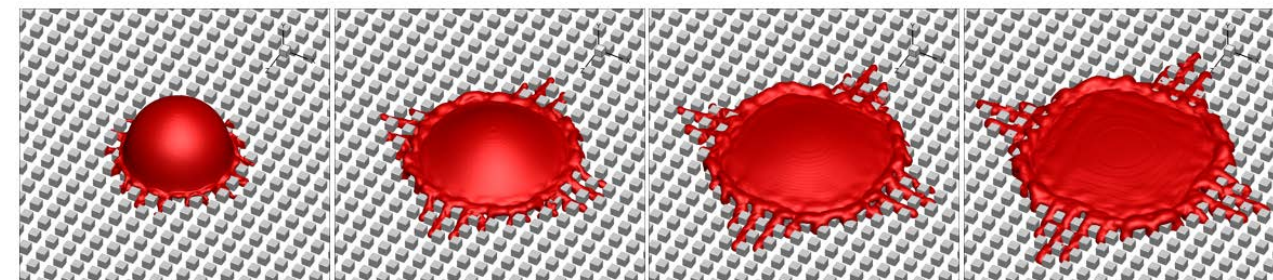
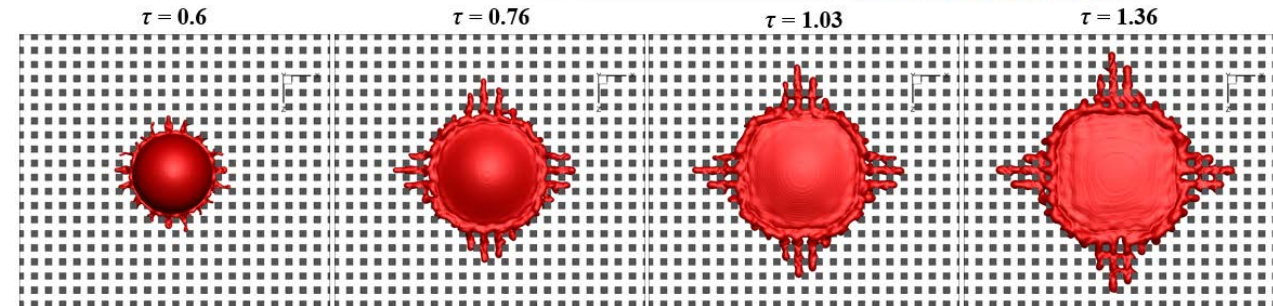
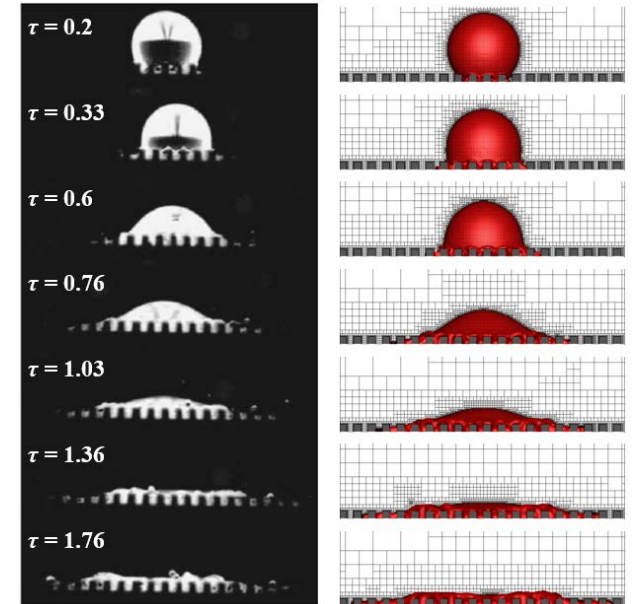
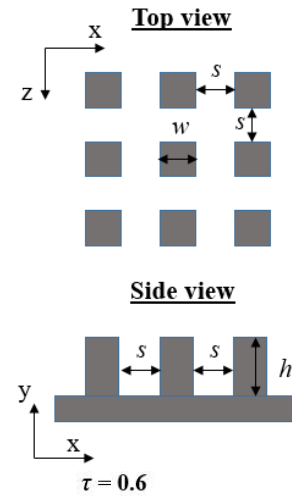
## Droplet impact on microstructured surfaces

Water droplets impact on substrates that consist of square-shaped pillars of  $w=0.3\text{mm}$   $h=0.3\text{mm}$   $s=0.3\text{mm}$  between pillars. (Sivakumar, et al. Physics of Fluids, 2005)

$D_o=2.99\text{mm}$ ,  
 $U_o=1.96\text{ m/s}$ . The  
 corresponding  
 $We=158.3$  and  
 $Re= 5895$



Robson and Willmott. Soft Matter, 2016

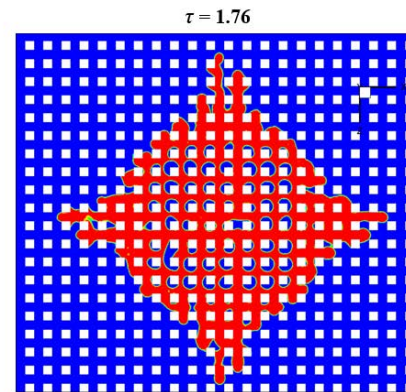
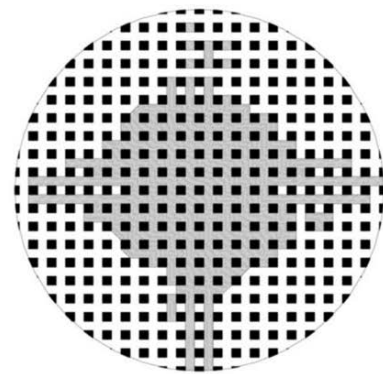
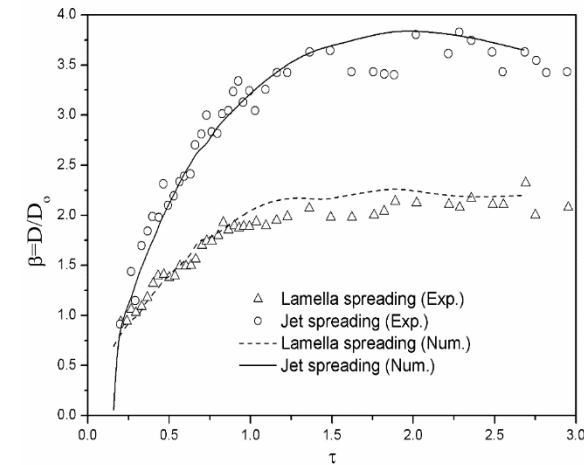
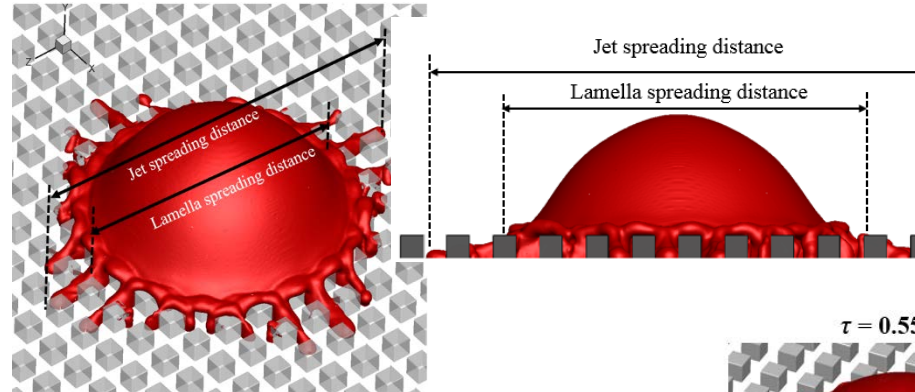


# Droplet-media interaction

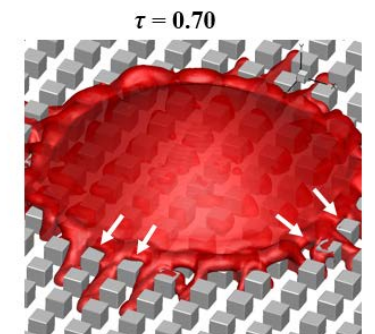
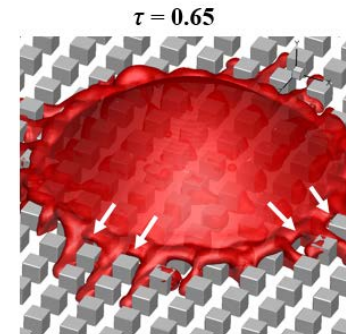
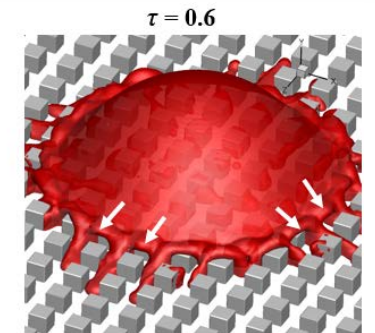
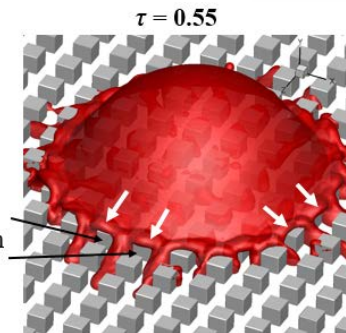
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$D_o=2.99\text{mm}$ ,  
 $U_o=1.96\text{ m/s}$ .  
 (We=158.3 and Re= 5895)



Space between current pillars and next ones in flow direction.

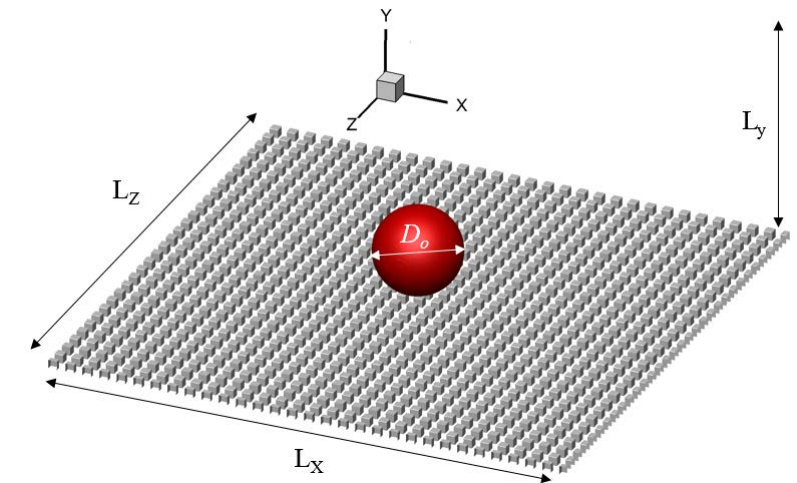
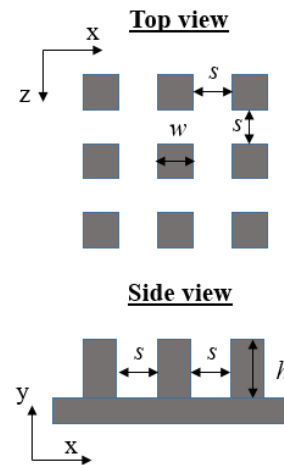
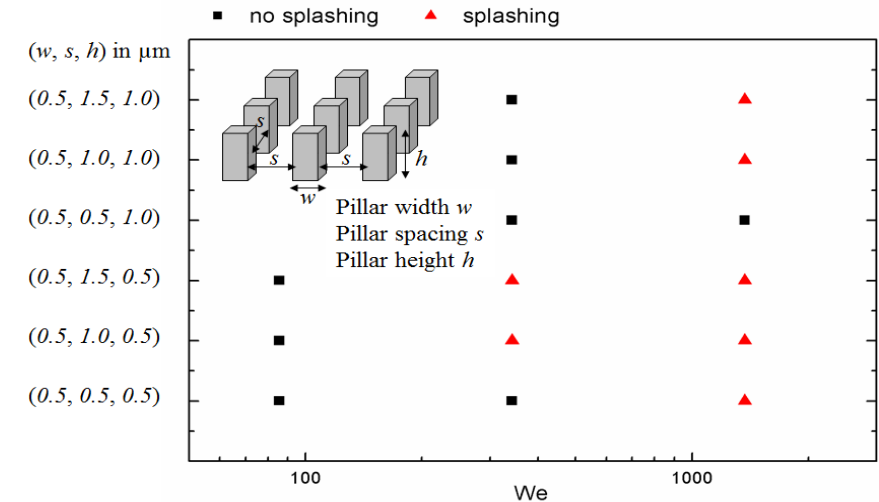


# Droplet-media interaction

## Droplet impact on microstructured surfaces\*

$D_o = 10 \mu\text{m}$

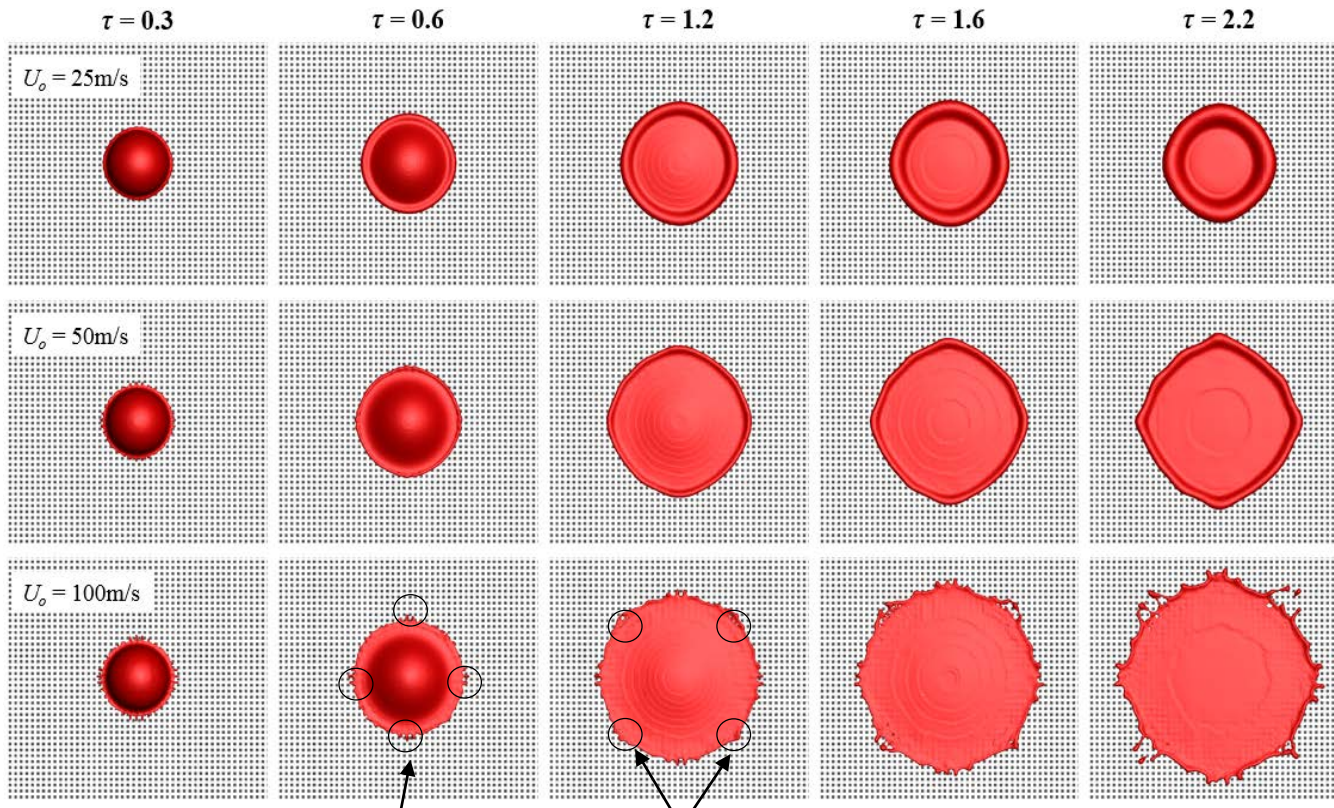
$U_o$ (m/s)	We	Re	w ( $\mu\text{m}$ )	s ( $\mu\text{m}$ )	h ( $\mu\text{m}$ )
25	86.6	250	0.5	0.5	0.5
			0.5	1.0	0.5
			0.5	1.5	0.5
50	342.5	500	0.5	0.5	0.5
			0.5	1.0	0.5
			0.5	1.5	0.5
			0.5	0.5	1.0
			0.5	1.0	1.0
			0.5	1.5	1.0
100	1369.9	1000	0.5	0.5	0.5
			0.5	1.0	0.5
			0.5	1.5	0.5
			0.5	0.5	1.0
			0.5	1.0	1.0
			0.5	1.5	1.0



\*H. Tan, Numerical study on splashing of high-speed microdroplet impact on dry microstructured surfaces. *Computers & Fluids*, 2017. **154**: p. 142-166.

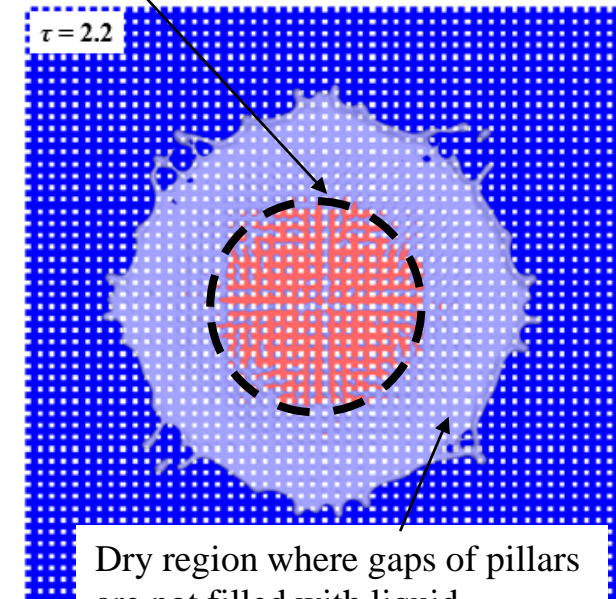
# Droplet-media interaction

**Effect of impact velocity** Snapshots of a droplet of  $D_o=10\ \mu\text{m}$  impact on the dry microstructured surface ( $s=h=w=0.5\ \mu\text{m}$ )

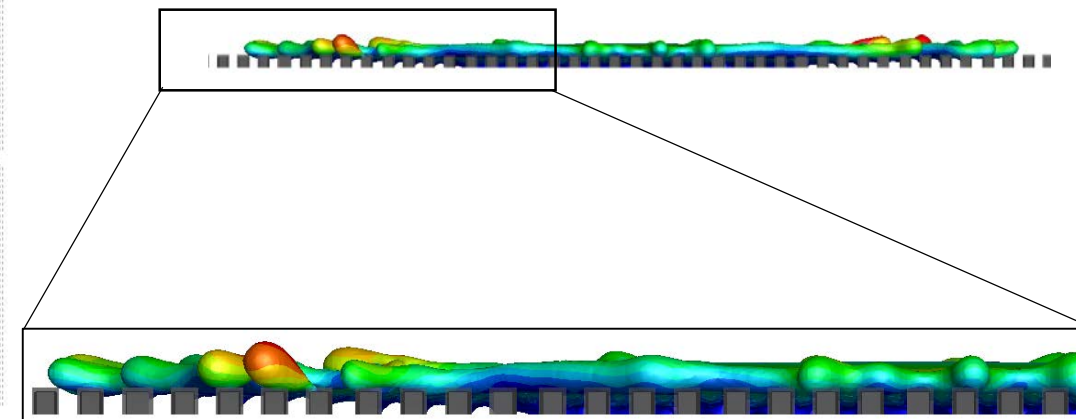


Jets in on-axis directions. Thin lamella becomes unstable.

Wetted region where gaps of pillars are nearly filled with liquid.



Dry region where gaps of pillars are not filled with liquid.





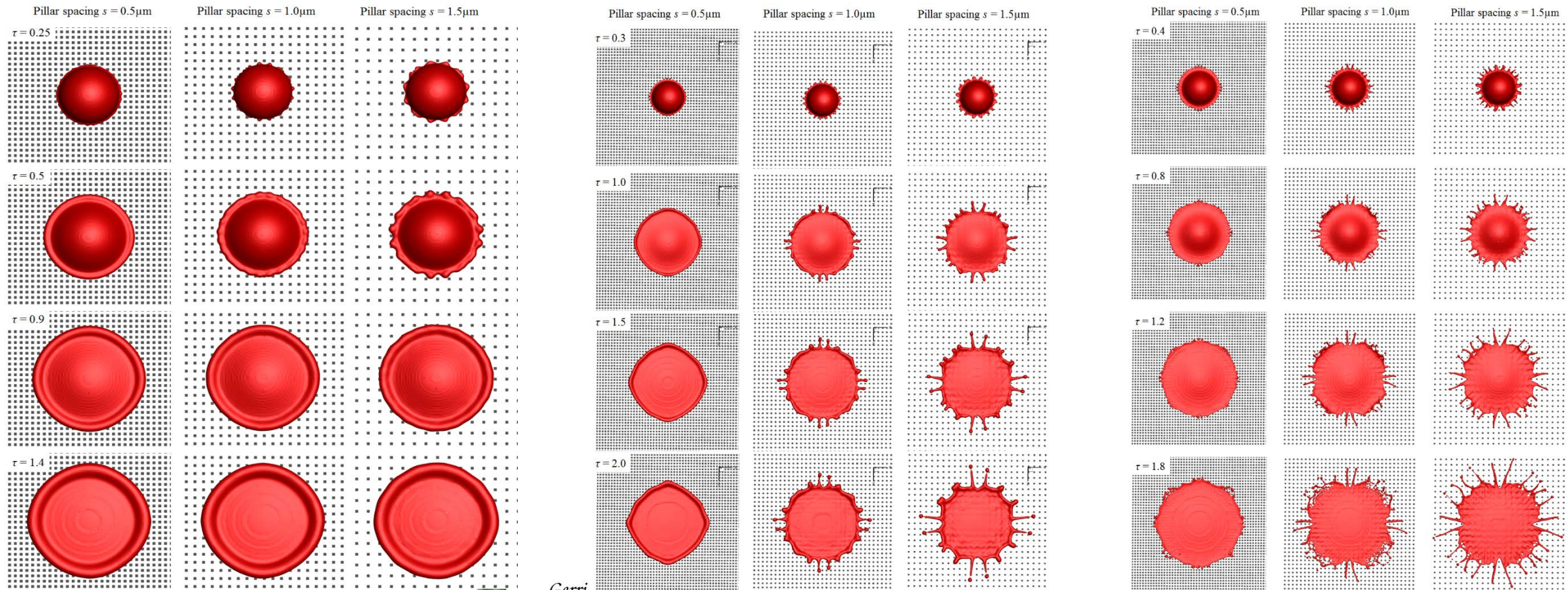
# Droplet-media interaction

## Effect of microstructures-Pillar spacing

$U_0 = 25$  m/s

$U_0 = 50$  m/s

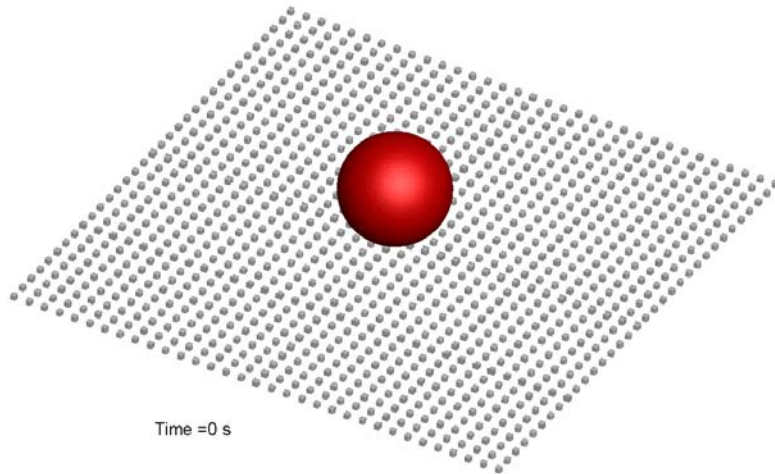
$U_0 = 100$  m/s



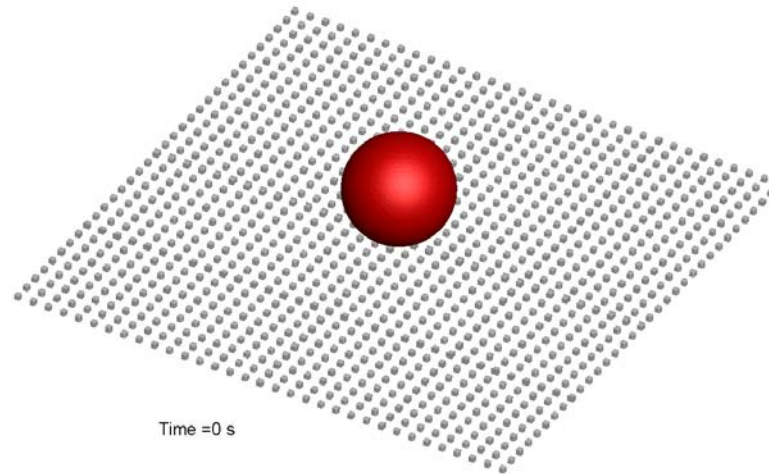
# Droplet-media interaction

## Droplet impact on microstructured surfaces\*

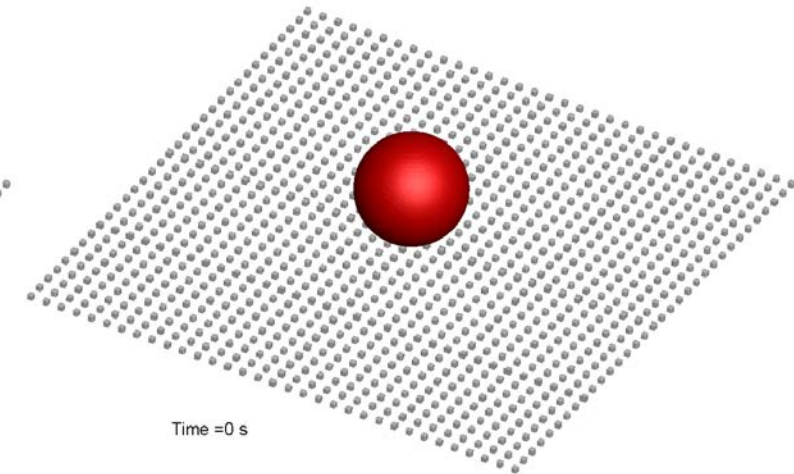
$U_o = 25$  m/s



$U_o = 50$  m/s



$U_o = 100$  m/s



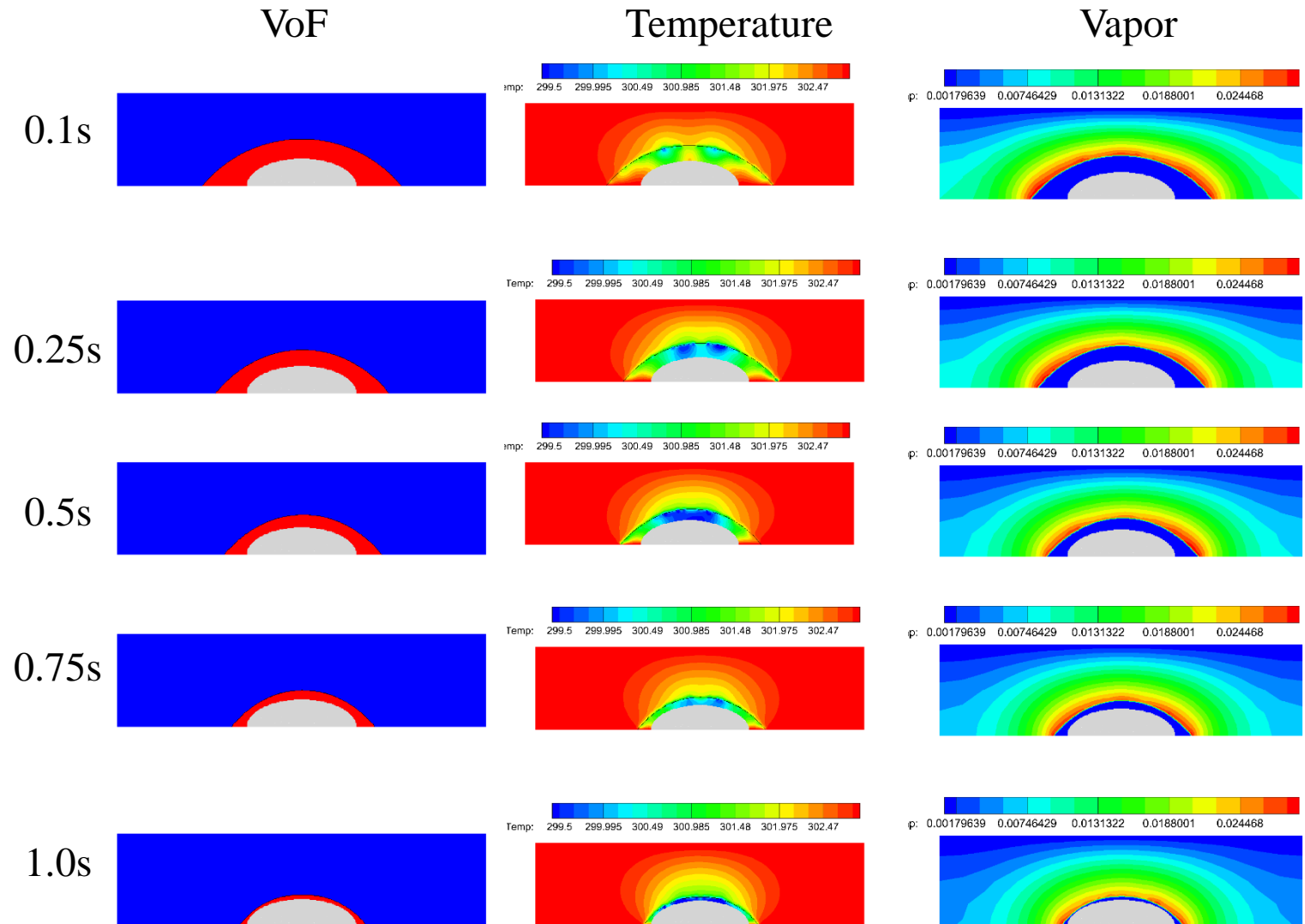
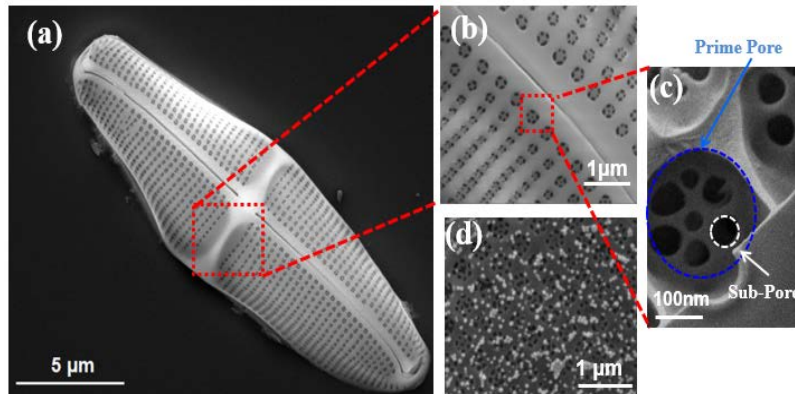
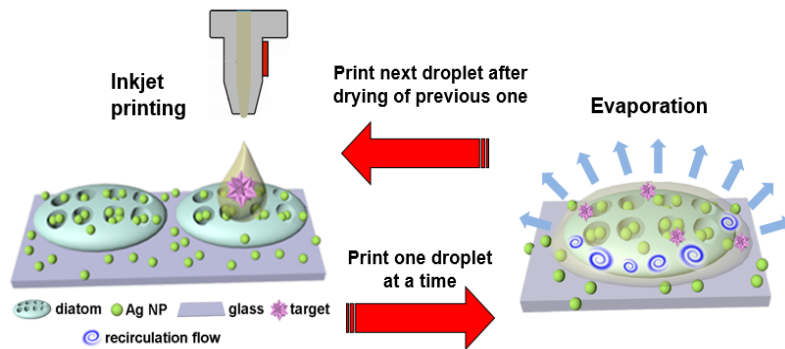
# Outline

- How do I get started with Gerris
- Droplet formation in Inkjet process
- Capillary flow in low-gravity
- Droplet-media interaction
- **Future work**



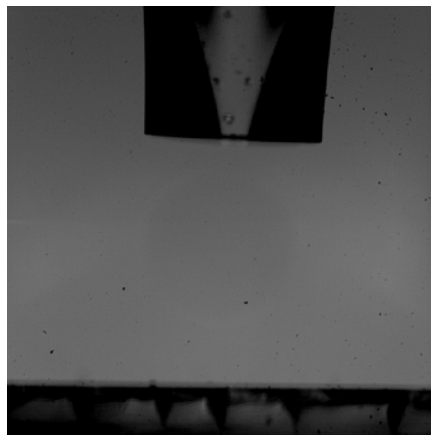
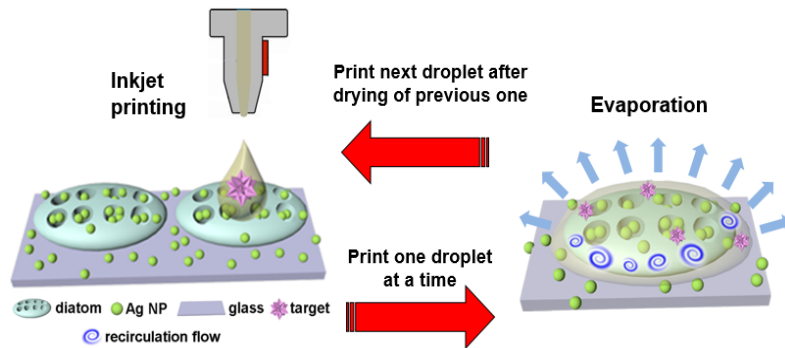
# Future work

## Thermocapillary flow\*

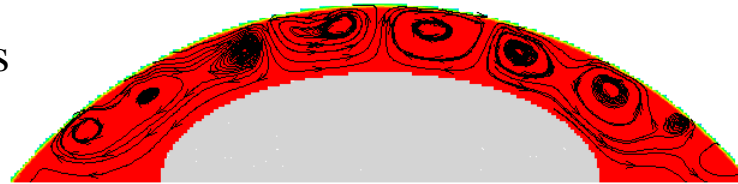


# Future work

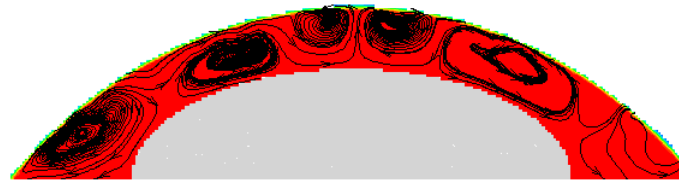
## Thermocapillary flow



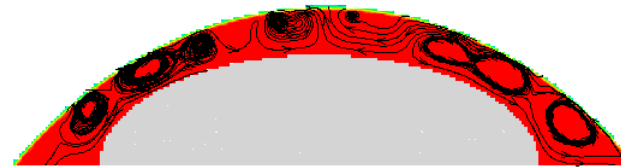
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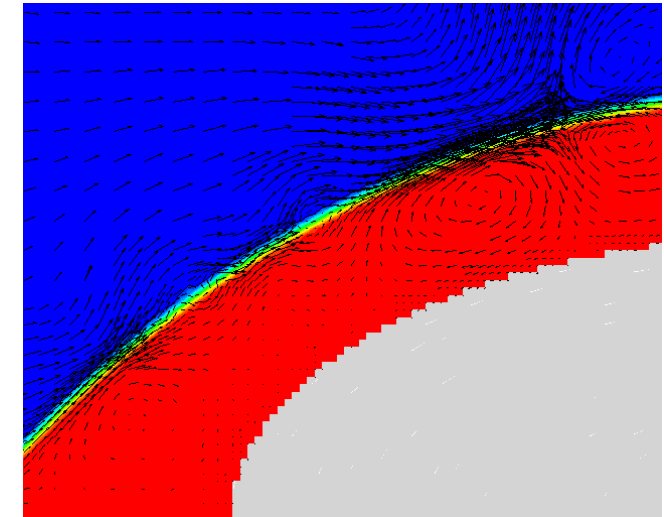
0.25s



0.5s



0.75s



# Thank you for your attention!

